

Please write clearly, in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

A-level FURTHER MATHEMATICS

Paper 1

Exam Date

Morning

Time allowed: 2 hours

Materials

For this paper you must have:

- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet. You do not necessarily need to use all the space provided.

Answer **all** questions in the spaces provided.

1 A vector is given by $\mathbf{a} = \begin{bmatrix} 2 \\ -1 \\ -3 \end{bmatrix}$

Which vector is **not** perpendicular to \mathbf{a} ?

Circle your answer.

[1 mark]

$$\begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 3 \\ 0 \\ 2 \end{bmatrix}$$

$$\begin{bmatrix} 5 \\ -1 \\ 3 \end{bmatrix}$$

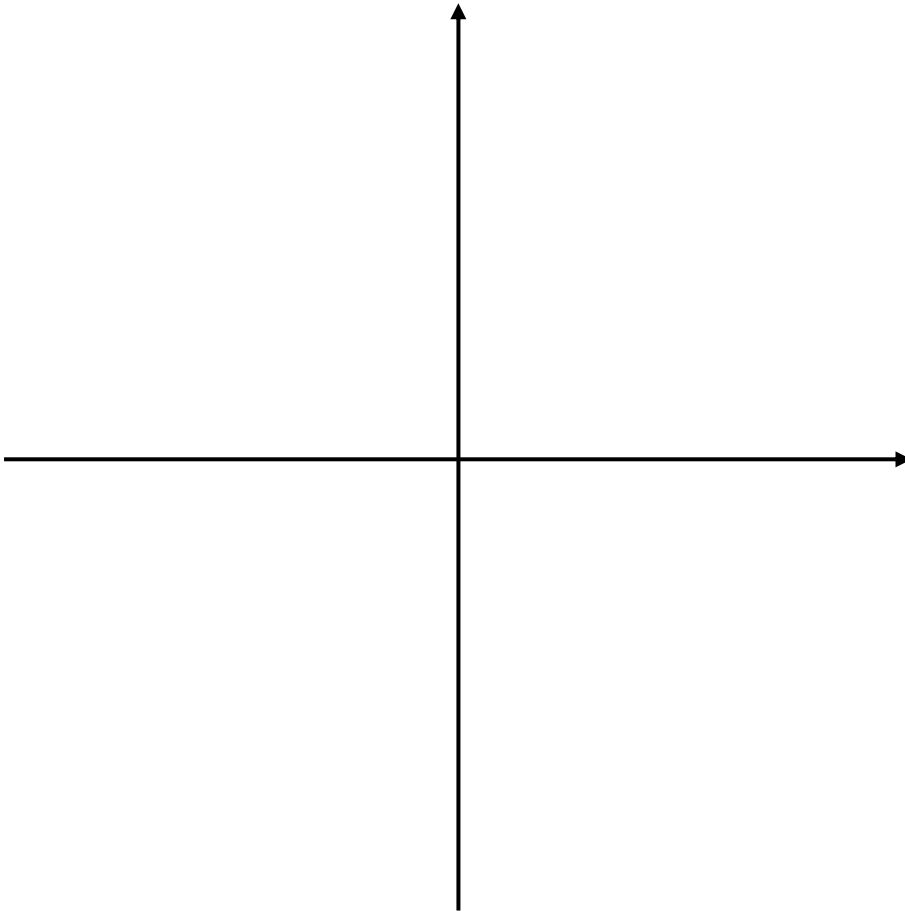
$$\begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix}$$

8 A curve has equation

$$y = \frac{5 - 4x}{1 + x}$$

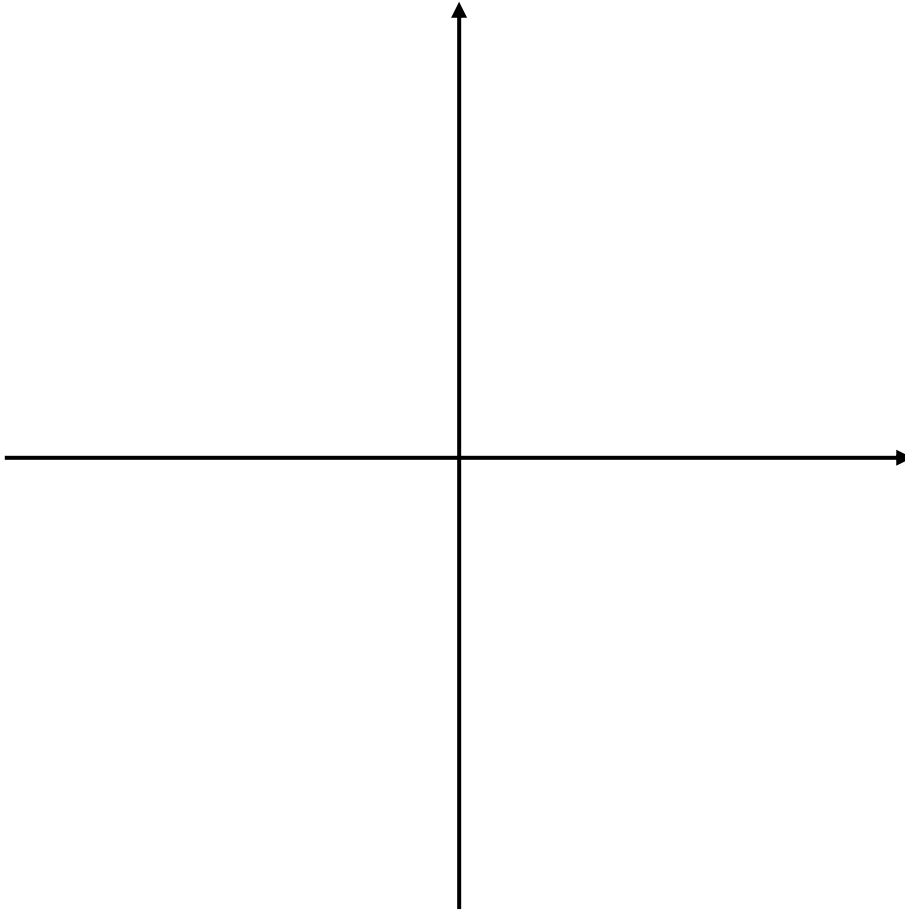
8 (a) Sketch the curve.

[4 marks]



8 (b) Hence sketch the graph of $y = \left| \frac{5 - 4x}{1 + x} \right|$.

[1 mark]



9 A line has Cartesian equations $x - p = \frac{y + 2}{q} = 3 - z$ and a plane has

equation $\mathbf{r} \cdot \begin{bmatrix} 1 \\ -1 \\ -2 \end{bmatrix} = -3$

9 (a) In the case where the plane fully contains the line, find the values of p and q .

[3 marks]

9 (b) In the case where the line intersects the plane at a single point, find the range of values of p and q .

[3 marks]

9 (c) In the case where the angle θ between the line and the plane satisfies $\sin\theta = \frac{1}{\sqrt{6}}$ and the line intersects the plane at $z = 0$

9 (c) (i) Find the value of q .

[4 marks]

9 (c) (ii) Find the value of p .

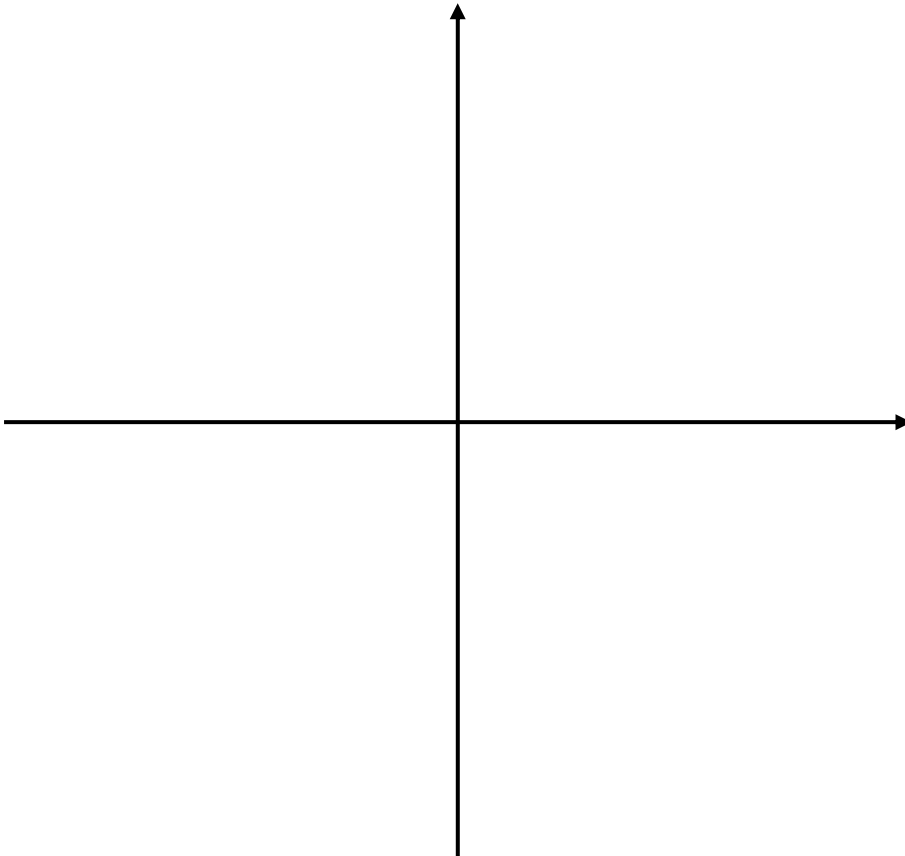
[3 marks]

10 The curve, C , has equation $y = \frac{x}{\cosh x}$

10 (a) Show that the x -coordinates of any stationary points of C satisfy the equation $\tanh x = \frac{1}{x}$
[3 marks]

10 (b) (i) Sketch the graphs of $y = \tanh x$ and $y = \frac{1}{x}$ on the axes below.

[2 marks]



15 (b) Suggest one way in which the model that you have used for the number of rabbits could be refined.

[1 mark]

END OF QUESTIONS