

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
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7	
8	
TOTAL	



General Certificate of Education  
Advanced Level Examination  
June 2010

# Mathematics

# MPC4

## Unit Pure Core 4

Tuesday 15 June 2010 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.



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QUESTION  
PART  
REFERENCE

Turn over ►



4 (a) (i) Find the binomial expansion of  $(1+x)^{\frac{3}{2}}$  up to and including the term in  $x^2$ .  
(2 marks)

(ii) Find the binomial expansion of  $(16+9x)^{\frac{3}{2}}$  up to and including the term in  $x^2$ .  
(3 marks)

(b) Use your answer to part (a)(ii) to show that  $13^{\frac{3}{2}} \approx 46 + \frac{a}{b}$ , stating the values of the integers  $a$  and  $b$ .  
(2 marks)

QUESTION  
PART  
REFERENCE







**5 (a) (i)** Show that the equation  $3 \cos 2x + 2 \sin x + 1 = 0$  can be written in the form

$$3 \sin^2 x - \sin x - 2 = 0 \quad (3 \text{ marks})$$

**(ii)** Hence, given that  $3 \cos 2x + 2 \sin x + 1 = 0$ , find the possible values of  $\sin x$ .  
(2 marks)

**(b) (i)** Express  $3 \cos 2x + 2 \sin 2x$  in the form  $R \cos(2x - \alpha)$ , where  $R > 0$  and  $0^\circ < \alpha < 90^\circ$ , giving  $\alpha$  to the nearest  $0.1^\circ$ .  
(3 marks)

**(ii)** Hence solve the equation

$$3 \cos 2x + 2 \sin 2x + 1 = 0$$

for all solutions in the interval  $0^\circ < x < 180^\circ$ , giving  $x$  to the nearest  $0.1^\circ$ .  
(3 marks)

QUESTION  
PART  
REFERENCE

A large rectangular area with horizontal dotted lines, intended for the student's answer.













8 (a) Solve the differential equation

$$\frac{dx}{dt} = -\frac{1}{5}(x + 1)^{\frac{1}{2}}$$

given that  $x = 80$  when  $t = 0$ . Give your answer in the form  $x = f(t)$ . (6 marks)

(b) A fungus is spreading on the surface of a wall. The proportion of the wall that is unaffected after time  $t$  hours is  $x\%$ . The rate of change of  $x$  is modelled by the differential equation

$$\frac{dx}{dt} = -\frac{1}{5}(x + 1)^{\frac{1}{2}}$$

At  $t = 0$ , the proportion of the wall that is unaffected is 80%. Find the proportion of the wall that will still be unaffected after 60 hours. (2 marks)

(c) A biologist proposes an alternative model for the rate at which the fungus is spreading on the wall. The total surface area of the wall is  $9 \text{ m}^2$ . The surface area that is **affected** at time  $t$  hours is  $A \text{ m}^2$ . The biologist proposes that the rate of change of  $A$  is proportional to the product of the surface area that is affected and the surface area that is unaffected.

(i) Write down a differential equation for this model.

(You are not required to solve your differential equation.) (2 marks)

(ii) A solution of the differential equation for this model is given by

$$A = \frac{9}{1 + 4e^{-0.09t}}$$

Find the time taken for 50% of the area of the wall to be affected. Give your answer in hours to three significant figures. (4 marks)

QUESTION  
PART  
REFERENCE

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**There are no questions printed on this page**

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ANSWER IN THE SPACES PROVIDED**

