

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education  
Advanced Level Examination  
June 2015

# Mathematics

# MFP3

## Unit Further Pure 3

Wednesday 13 May 2015 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

- Instructions**
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
  - Fill in the boxes at the top of this page.
  - Answer **all** questions.
  - Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
  - You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
  - Do not write outside the box around each page.
  - Show all necessary working; otherwise marks for method may be lost.
  - Do all rough work in this book. Cross through any work that you do not want to be marked.

- Information**
- The marks for questions are shown in brackets.
  - The maximum mark for this paper is 75.

- Advice**
- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
  - You do not necessarily need to use all the space provided.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
<b>TOTAL</b>	



J U N 1 5 M F P 3 0 1

Answer **all** questions.

Answer each question in the space provided for that question.

**1** It is given that  $y(x)$  satisfies the differential equation

$$\frac{dy}{dx} = f(x, y)$$

where  $f(x, y) = \frac{x + y^2}{x}$

and  $y(2) = 5$

**(a)** Use the Euler formula

$$y_{r+1} = y_r + hf(x_r, y_r)$$

with  $h = 0.05$ , to obtain an approximation to  $y(2.05)$ .

**[2 marks]**

**(b)** Use the formula

$$y_{r+1} = y_{r-1} + 2hf(x_r, y_r)$$

with your answer to part **(a)**, to obtain an approximation to  $y(2.1)$ , giving your answer to three significant figures.

**[3 marks]**

QUESTION  
PART  
REFERENCE

**Answer space for question 1**



QUESTION  
PART  
REFERENCE

**Answer space for question 1**

A large rectangular area containing horizontal dotted lines for writing an answer.



**Turn over ►**



QUESTION  
PART  
REFERENCE

**Answer space for question 2**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



**3 (a) (i)** Write down the expansion of  $\ln(1 + 2x)$  in ascending powers of  $x$  up to and including the term in  $x^4$ .

[1 mark]

**(ii)** Hence, or otherwise, find the first two non-zero terms in the expansion of

$$\ln[(1 + 2x)(1 - 2x)]$$

in ascending powers of  $x$  and state the range of values of  $x$  for which the expansion is valid.

[3 marks]

**(b)** Find  $\lim_{x \rightarrow 0} \left[ \frac{3x - x\sqrt{9+x}}{\ln[(1+2x)(1-2x)]} \right]$ .

[4 marks]

QUESTION  
PART  
REFERENCE

**Answer space for question 3**



QUESTION  
PART  
REFERENCE

**Answer space for question 3**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



4 (a) Explain why  $\int_2^{\infty} (x - 2)e^{-2x} dx$  is an improper integral.

[1 mark]

(b) Evaluate  $\int_2^{\infty} (x - 2)e^{-2x} dx$ , showing the limiting process used.

[6 marks]

QUESTION  
PART  
REFERENCE

Answer space for question 4





QUESTION  
PART  
REFERENCE

**Answer space for question 4**

A large rectangular area with horizontal dotted lines for writing an answer.





QUESTION  
PART  
REFERENCE

**Answer space for question 5**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



QUESTION  
PART  
REFERENCE

**Answer space for question 5**

A large rectangular area containing horizontal dotted lines for writing an answer.



QUESTION  
PART  
REFERENCE

**Answer space for question 5**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**





QUESTION  
PART  
REFERENCE

**Answer space for question 6**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



QUESTION  
PART  
REFERENCE

**Answer space for question 6**

A large rectangular area containing horizontal dotted lines for writing an answer.





QUESTION  
PART  
REFERENCE

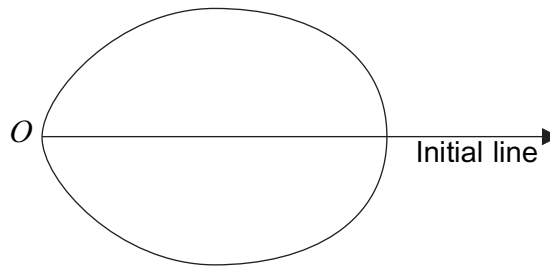
**Answer space for question 6**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



- 7 The diagram shows the sketch of a curve  $C_1$ .



The polar equation of the curve  $C_1$  is

$$r = 1 + \cos 2\theta, \quad -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

- (a) Find the area of the region bounded by the curve  $C_1$ .

[5 marks]

- (b) The curve  $C_2$  whose polar equation is

$$r = 1 + \sin \theta, \quad -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

intersects the curve  $C_1$  at the pole  $O$  and at the point  $A$ . The straight line drawn through  $A$  parallel to the initial line intersects  $C_1$  again at the point  $B$ .

- (i) Find the polar coordinates of  $A$ .

[4 marks]

- (ii) Show that the length of  $OB$  is  $\frac{1}{4}(\sqrt{13} + 1)$ .

[6 marks]

- (iii) Find the length of  $AB$ , giving your answer to three significant figures.

[3 marks]

QUESTION  
PART  
REFERENCE

Answer space for question 7



QUESTION  
PART  
REFERENCE

**Answer space for question 7**

A large rectangular area with horizontal dotted lines for writing an answer.

**Turn over ►**



QUESTION  
PART  
REFERENCE

**Answer space for question 7**

A large rectangular area containing horizontal dotted lines for writing an answer.



QUESTION  
PART  
REFERENCE

**Answer space for question 7**

A large rectangular area with horizontal dotted lines for writing an answer.

**END OF QUESTIONS**



**There are no questions printed on this page**

**DO NOT WRITE ON THIS PAGE  
ANSWER IN THE SPACES PROVIDED**



**There are no questions printed on this page**

**DO NOT WRITE ON THIS PAGE  
ANSWER IN THE SPACES PROVIDED**



**There are no questions printed on this page**

**DO NOT WRITE ON THIS PAGE  
ANSWER IN THE SPACES PROVIDED**

Copyright © 2015 AQA and its licensors. All rights reserved.

