

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

AS MATHEMATICS

Unit Further Pure 1

Wednesday 15 June 2016

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



Answer **all** questions.

Answer each question in the space provided for that question.

1 The quadratic equation $x^2 - 6x + 14 = 0$ has roots α and β .

(a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$.

[2 marks]

(b) Find a quadratic equation, with integer coefficients, which has roots $\frac{\alpha}{\beta}$ and $\frac{\beta}{\alpha}$.

[5 marks]

QUESTION
PART
REFERENCE

Answer space for question 1



- 2** A curve C has equation $y = (2 - x)(1 + x) + 3$.
- (a)** A line passes through the point $(2, 3)$ and the point on C with x -coordinate $2 + h$.
Find the gradient of the line, giving your answer in its simplest form. **[3 marks]**
- (b)** Show how your answer to part **(a)** can be used to find the gradient of the curve C at the point $(2, 3)$. State the value of this gradient. **[2 marks]**

QUESTION
PART
REFERENCE**Answer space for question 2**

- 3 The variables y and x are related by an equation of the form

$$y = a(b^x)$$

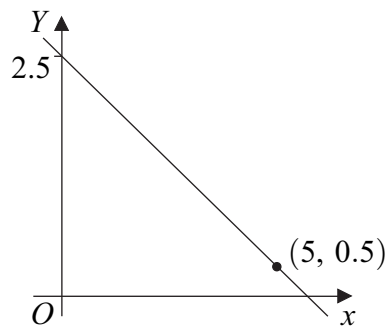
where a and b are positive constants.

Let $Y = \log_{10} y$.

- (a) Show that there is a linear relationship between Y and x .

[2 marks]

- (b) The graph of Y against x , shown below, passes through the points $(0, 2.5)$ and $(5, 0.5)$.



- (i) Find the gradient of the line.

[1 mark]

- (ii) Find the value of a and the value of b , giving each answer to three significant figures.

[4 marks]

QUESTION
PART
REFERENCE

Answer space for question 3



4 (a) Given that $\sin \frac{\pi}{3} = \cos \frac{\pi}{k}$, state the value of the integer k .

[1 mark]

(b) Hence, or otherwise, find the general solution of the equation

$$\cos\left(2x - \frac{5\pi}{6}\right) = \sin \frac{\pi}{3}$$

giving your answer, in its simplest form, in terms of π .

[4 marks]

(c) Hence, given that $\cos\left(2x - \frac{5\pi}{6}\right) = \sin \frac{\pi}{3}$, show that there is only one finite value for $\tan x$ and state its exact value.

[2 marks]

QUESTION
PART
REFERENCE

Answer space for question 4



5 (a) Use the formulae for $\sum_{r=1}^n r^2$ and $\sum_{r=1}^n r$ to show that $\sum_{r=1}^n (6r - 3)^2 = 3n(4n^2 - 1)$.

[5 marks]

(b) Hence express $\sum_{r=1}^{2n} r^3 - \sum_{r=1}^n (6r - 3)^2$ as a product of four linear factors in terms of n .

[4 marks]

QUESTION
PART
REFERENCE

Answer space for question 5



6 A parabola with equation $y^2 = 4ax$, where a is a constant, is translated by the vector $\begin{bmatrix} 2 \\ 3 \end{bmatrix}$ to give the curve C . The curve C passes through the point $(4, 7)$.

(a) Show that $a = 2$.

[3 marks]

(b) Find the values of k for which the line $ky = x$ does **not** meet the curve C .

[6 marks]

QUESTION
PART
REFERENCE

Answer space for question 6



8 The matrix \mathbf{A} is defined by $\mathbf{A} = \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix}$.

(a) (i) Find the matrix \mathbf{A}^2 .

[1 mark]

(ii) Describe fully the single geometrical transformation represented by the matrix \mathbf{A}^2 .

[1 mark]

(b) Given that the matrix \mathbf{B} represents a reflection in the line $x + \sqrt{3}y = 0$, find the matrix \mathbf{B} , giving the exact values of any trigonometric expressions.

[2 marks]

(c) Hence find the coordinates of the point P which is mapped onto $(0, -4)$ under the transformation represented by \mathbf{A}^2 followed by a reflection in the line $x + \sqrt{3}y = 0$.

[6 marks]

QUESTION
PART
REFERENCE

Answer space for question 8



9 A curve C has equation $y = \frac{x-1}{(x-2)(2x-1)}$.

The line L has equation $y = \frac{1}{2}(x-1)$.

(a) Write down the equations of the asymptotes of C . [2 marks]

(b) By forming and solving a suitable cubic equation, find the x -coordinates of the points of intersection of L and C . [3 marks]

(c) Given that C has no stationary points, sketch C and L on the same axes. [3 marks]

(d) Hence solve the inequality $\frac{x-1}{(x-2)(2x-1)} \geq \frac{1}{2}(x-1)$. [3 marks]

QUESTION
PART
REFERENCE

Answer space for question 9



