

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

AS MATHEMATICS

Unit Pure Core 2

Wednesday 25 May 2016

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



Answer **all** questions.

Answer each question in the space provided for that question.

1 (a) Find $\int \left(\frac{36}{x^2} + ax \right) dx$, where a is a constant.

[3 marks]

(b) Hence, given that $\int_1^3 \left(\frac{36}{x^2} + ax \right) dx = 16$, find the value of the constant a .

[2 marks]

QUESTION
PART
REFERENCE

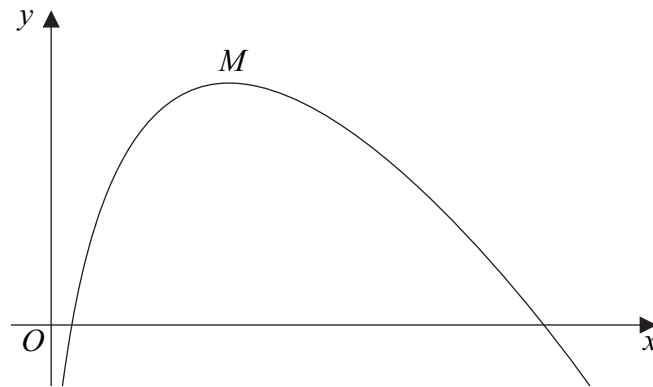
Answer space for question 1



- 2 (a)** Sketch the graph of $y = (0.2)^x$, indicating the value of the intercept on the y -axis. **[2 marks]**
- (b)** Use logarithms to solve the equation $(0.2)^x = 4$, giving your answer to three significant figures. **[2 marks]**
- (c)** Describe the geometrical transformation that maps the graph of $y = (0.2)^x$ onto the graph of $y = 5^x$. **[1 mark]**

QUESTION
PART
REFERENCE**Answer space for question 2**

- 3 The diagram shows a curve with a maximum point M .



The curve is defined for $x > 0$ by the equation

$$y = 6x^{\frac{1}{2}} - x - 3$$

- (a) Find $\frac{dy}{dx}$. [2 marks]
- (b) Hence find the y -coordinate of the maximum point M . [3 marks]
- (c) Find an equation of the normal to the curve at the point $P(4, 5)$. [3 marks]
- (d) It is given that the normal to the curve at P , when translated by the vector $\begin{bmatrix} k \\ 0 \end{bmatrix}$, passes through the point M . Find the value of the constant k . [3 marks]

QUESTION
PART
REFERENCE

Answer space for question 3



5 (a) Use the trapezium rule with four ordinates (three strips) to find an approximate value for $\int_2^{11} \sqrt{x^2 + 9} dx$. Give your answer to one decimal place.

[4 marks]

(b) Describe the geometrical transformation that maps the graph of $y = \sqrt{x^2 + 9}$ onto the graph of :

(i) $y = 5 + \sqrt{x^2 + 9}$;

[2 marks]

(ii) $y = 3\sqrt{x^2 + 1}$.

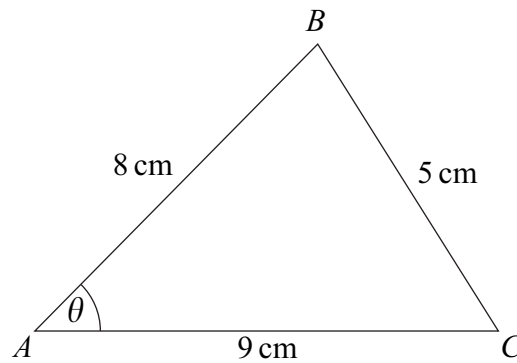
[2 marks]

QUESTION
PART
REFERENCE

Answer space for question 5



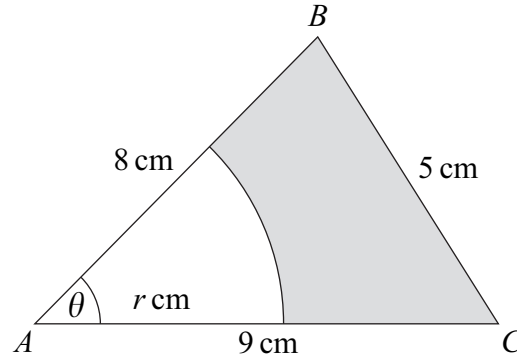
- 6 The diagram shows a triangle ABC .



The lengths of AB , BC and AC are 8 cm, 5 cm and 9 cm respectively.

Angle BAC is θ radians.

- (a) Show that $\theta = 0.586$, correct to three significant figures. [3 marks]
- (b) Find the area of triangle ABC , giving your answer, in cm^2 , to three significant figures. [2 marks]
- (c) A circular sector, centre A and radius r cm, is removed from triangle ABC . The remaining shape is shown shaded in the diagram below.



Given that the area of the sector removed is equal to the area of the shaded shape, find the perimeter of the shaded shape. Give your answer in cm to three significant figures.

[6 marks]

QUESTION
PART
REFERENCE

Answer space for question 6



7 (a) The expression $(1 - 2x)^5$ can be written in the form

$$1 + px + qx^2 + rx^3 + 80x^4 - 32x^5$$

By using the binomial expansion, or otherwise, find the values of the coefficients p , q and r .

[3 marks]

(b) Find the value of the coefficient of x^{10} in the expansion of $(1 - 2x)^5(2 + x)^7$.

[5 marks]

QUESTION
PART
REFERENCE

Answer space for question 7



8 (a) (i) Given that $4 \sin x + 5 \cos x = 0$, find the value of $\tan x$.

[2 marks]

(ii) Hence solve the equation $(1 - \tan x)(4 \sin x + 5 \cos x) = 0$ in the interval $0^\circ \leq x \leq 360^\circ$, giving your values of x to the nearest degree.

[3 marks]

(b) By first showing that $\frac{16 + 9 \sin^2 \theta}{5 - 3 \cos \theta}$ can be expressed in the form $p + q \cos \theta$, where p and q are integers, find the least possible value of $\frac{16 + 9 \sin^2 \theta}{5 - 3 \cos \theta}$.

State the exact value of θ , in radians in the interval $0 \leq \theta < 2\pi$, at which this least value occurs.

[4 marks]

QUESTION
PART
REFERENCE

Answer space for question 8



9 (a) Given that $\log_3 c = m$ and $\log_{27} d = n$, express $\frac{\sqrt{c}}{d^2}$ in the form 3^y , where y is an expression in terms of m and n .

[4 marks]

(b) Show that the equation

$$\log_4(2x + 3) + \log_4(2x + 15) = 1 + \log_4(14x + 5)$$

has only one solution and state its value.

[4 marks]

QUESTION
PART
REFERENCE**Answer space for question 9**

