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FUNCTIONAL SKILLS CERTIFICATE  
**Functional Mathematics**

Level 2

Mark Scheme

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4368

November 2016

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Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from [aqa.org.uk](http://aqa.org.uk)

## Glossary for Mark Schemes

Examinations are marked to award positive achievement.

Marks are awarded for demonstrating the following interrelated **process skills**.

**Representing** Selecting the mathematics and information to model a situation.

- R.1** Candidates recognise that a situation has aspects that can be represented using mathematics.
- R.2** Candidates make an initial model of a situation using suitable forms of representation.
- R.3** Candidates decide on the methods, operations and tools, including ICT, to use in a situation.
- R.4** Candidates select the mathematical information to use.

**Analysing** Processing and using mathematics.

- A.1** Candidates use appropriate mathematical procedures.
- A.2** Candidates examine patterns and relationships.
- A.3** Candidates change values and assumptions or adjust relationships to see the effects on answers in models.
- A.4** Candidates find results and solutions.

**Interpreting** Interpreting and communicating the results of the analysis.

- I.1** Candidates interpret results and solutions.
- I.2** Candidates draw conclusions in light of situations.
- I.3** Candidates consider the appropriateness and accuracy of results and conclusions.
- I.4** Candidates choose appropriate language and forms of presentation to communicate results and solutions.

In particular, individual marks are mapped onto the following **skills standards**.

**Representing** Making sense of the situations and representing them.

A learner can:

- Ra** Understand routine and non-routine problems in familiar and unfamiliar contexts and situations.
- Rb** Identify the situation or problems and identify the mathematical methods needed to solve them.
- Rc** Choose from a range of mathematics to find solutions.

**Analysing** Processing and using the mathematics.

A learner can:

- Aa** Apply a range of mathematics to find solutions.
- Ab** Use appropriate checking procedures and evaluate their effectiveness at each stage.

**Interpreting** Interpreting and communicating the results of the analysis.

A learner can:

- Ia** Interpret and communicate solutions to multistage practical problems in familiar and unfamiliar contexts and situations.
- Ib** Draw conclusions and provide mathematical justifications.

To facilitate marking, the following categories are used:

- M** Method marks are awarded for a correct method which could lead to a correct answer.
- A** Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- B** Marks awarded independent of method.
- ft** Follow through marks. Marks awarded following a mistake in an earlier step.
- SC** Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- oe** Or equivalent. Accept answers that are equivalent.  
eg, accept 0.5 as well as  $\frac{1}{2}$

Q	Answer		Mark	Comments
1 (a)	their $270 \div 0.5$ or their $270 \times 2$ or 540	or their $24 \div 0.3$ or 80	M1 Ra	
	540 or 620		A1 Rc	
	200 + 15 × 2 or 230		M1 Aa	
	100 + 100 + 100 + their 230		M1 Aa	Allow one error but must include 4 exits only - <b>not</b> the 1250 mm exit
	530		A1 Rc	
	Clearly identifies the lower of their 540 or 620 and their 530		A1ft lb	ft from 1 <sup>st</sup> and 3 <sup>rd</sup> M marks

1 (b)	600 – 3 × 80 or 600 – 240 or 360	M1 Ra	
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Q	Answer	Mark	Comments
	their $360 \div (5 + 4) \times 5$ or $40 \times 5$ or 200 or their $360 \div (5 + 4) \times 4$ or $40 \times 4$ or 160	M1  Rc	
	Liz → £200 and Omar → £160	A1 Ia	Must see £ symbol and names SC2 Liz → £333.33 and Omar → £267.67 SC1 333.33 and 267.67
<b>Check</b>	their $200 \div 5 = 40$ and their $160 \div 4 = 40$ or their $200 \div 40 = 5$ and their $160 \div 40 = 4$ or $200 : 160 = 5 \times 40 : 4 \times 40$	B1ft Ab	
	<b>Additional Guidance</b>		
	To award the mark for the check must show a clear understanding of ratio		

	<b>Alternative method 1</b>		
<b>1 (c)</b>	$70 \div 40$ or 1.75 or 1 hour 45 minutes	M1 Ra	

Q	Answer	Mark	Comments	
	their 1 hour 45 minutes + 50 minutes or 2 hours 35 minutes	M1 <i>Aa</i>	5.30 + their 1 hour 45 minutes or 7.15	
	5.30 + their 2 hours 35 minutes	M1 <i>Rc</i>	their 7.15 + 50 minutes	8.00 – 50 minutes
	8.05 and No or 7.15 and 7.10 and No	A2 <i>lb</i>	A1 8.05 or 7.15 and 7.10 or A1ft correct decision for their values (only if M3 scored)	
<b>Alternative method 2</b>				
	70 ÷ 40 or 1.75 or 1 hour 45 minutes	M1 <i>Ra</i>		
	their 1 hour 45 minutes + 50 minutes or 2 hours 35 minutes	M1 <i>Aa</i>	8.00 – 50 minutes or 7.10	
	8.00 – their 2 hour 35 minutes	M1 <i>Rc</i>	their 7.10 – their 1 hour 45 minutes	5.30 + their 1 hour 45 minutes
	5.25 and No or 7.15 and 7.10 and No	A2 <i>lb</i>	A1 5.25 or 7.15 and 7.10 or A1ft correct decision for their values (only if M3 scored)	

<b>1(c)</b>	<b>Alternative method 3</b>			
		M1 <i>Ra</i>		
	their 1 hour 45 minutes + 50 minutes	M1		

Q	Answer	Mark	Comments
	or 2 hours 35 minutes		
	8.00 – 5.30 or 2 hours 30 minutes	M1 Rc	
	2 hours 35 minutes and 2 hours 30 minutes and No	A2 Ib	A1 2 hours 35 minutes and 2 hours 30 minutes or A1ft correct decision for their values (only if M3 scored)

**Additional Guidance**

**Other alternatives**

There are other alternative mark schemes, e.g. showing that the actual speed to arrive on time > 40 mph

Arrival time 7.10

Journey time 1 hour 40 minutes (1.66 ... hours)

Required speed  $70 \div 1.66 \dots = 42$  mph

**Decimal times**

Students who convert between a time as a decimal to hours and minutes incorrectly (or vice versa) can score method marks only.

e.g. their 1.75 hours = 2 hours 15 minutes from 1.75 hours  $\rightarrow$  1 hour 75 minutes

e.g 1.75 hours + 50 minutes = 2 hours 25 minutes from  $1.75 + 0.50 \rightarrow 2.25$



Q	Answer	Mark	Comments
2 (a)	560	B1 Aa	

2 (b)	<b>Alternative method 1</b>		
	$300 \div 750$ or $\frac{2}{5}$ or 0.4	M1 Ra	or $750 \div 300$ or 2.5
	their $\frac{2}{5} \times 60$ or their $0.4 \times 60$	M1 Rc	or $60 \div 2.5$
	24	A1 Aa	
	<b>Alternative method 2</b>		
	$750 \div 60$ or 12.5	M1 Ra	calories per minute
	$300 \div$ their 12.5	M1 Rc	
	24	A1 Aa	
Check	reverse or alt method e.g. $24 \div 60 \times 750 = 300$ or $300 \div 24 \times 60 = 750$ or $24 \times 12.5 = 300$ and $60 \times 12.5 = 750$	B1ft Ab	
2 (b)	<b>Additional Guidance</b>		
	<b>Misread</b> Award a maximum of M2 for any other value from table used instead of 750, eg $840 \div 60 = 14$ $300 \div 14$ 21.4		M1 M1 A0
	Award marks for main question if working/answer seen in Check		

Q	Answer	Mark	Comments																				
<b>2 (c)</b>	works out correct calories for given time for one machine	B1 Aa	any time for any machine level can be omitted																				
	attempts to work out calories for each of three or four different machines compatible with specified level and time	B1 Aa	level and time must be given – level can be implied from calories per hour either level except for stair climber which must be at level 1 must use a correct method but allow numerical slips																				
	between 5 and 20 minutes on all machines chosen	B1 la la	must be at least 3 machines																				
	their total calories for all machines chosen between 850 and 1000	B1ft la la	ft correct method for calories only does not need to be given must be at least 3 machines																				
	total time 60 minutes	B1 Aa	does not need to be given must be 4 machines																				
	fully correct plan clearly communicated using all four machines	B2 la la	B1 plan using all four machines with up to two errors/omissions																				
<b>Additional Guidance</b>																							
<table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>Treadmill</td> <td>Level 2</td> <td>15 min</td> <td>225 calories</td> </tr> <tr> <td>Bike</td> <td>Level 2</td> <td>20 min</td> <td>280 calories</td> </tr> <tr> <td>Stair climber</td> <td>Level 1</td> <td>10 min</td> <td>160 calories</td> </tr> <tr> <td>Rower</td> <td>Level 2</td> <td>15 min</td> <td>262.5 calories</td> </tr> <tr> <td colspan="2" style="text-align: center;">Totals</td> <td>60 min</td> <td>927.5 calories</td> </tr> </tbody> </table> <p>For fully correct plan (for B2) must see                      Use of at least one of each machine                      all times between 5 minutes and 20 minutes (inclusive)                      levels for each machine with Level 1 for the stair climber                      all times totalling 60 minutes (total need not be given)                      correct calories for each machine (compatible with time and level)                      correct total calories between 850 and 1000 (total need not be given)</p> <p>Examples of errors and omissions                      number of calories incompatible with level and/or time                      one Level missing or Stair climber used at Level 2                      total time not 60 minutes                      total calories out of given range</p> <p>Wrong method for calculating calories (all machines) can score B0B0B1B0B1B0 max                      Not giving levels (all machines) can score B1B0B1B1B1B0 max                      Not giving levels or times can score 1<sup>st</sup> B1 only                      Using stair climber at Level 2 can score B1B1B1B1B1B1</p>				Treadmill	Level 2	15 min	225 calories	Bike	Level 2	20 min	280 calories	Stair climber	Level 1	10 min	160 calories	Rower	Level 2	15 min	262.5 calories	Totals		60 min	927.5 calories
Treadmill	Level 2	15 min	225 calories																				
Bike	Level 2	20 min	280 calories																				
Stair climber	Level 1	10 min	160 calories																				
Rower	Level 2	15 min	262.5 calories																				
Totals		60 min	927.5 calories																				

Q	Answer	Mark	Comments
2 (d)	$30 \times 2.5$ or $30 + 30 + 15$ or 75	M1 Ra	
	$180 \div 4$ or 45	M1 Rb	
	their 75 + their 45 + 112 or $250 - \text{their } 75 - \text{their } 45 - 112$	M1 Aa	can be implied from correct totals
	$75 + 45 + 112 = 232$ or $250 - 75 - 45 - 112 = 18$	A1 Ib	
	<b>Additional Guidance</b>		
Award 4 marks if 232 seen with no working			

Q	Answer	Mark	Comments
3 (a)	any one of patio, vegetable patch, lawn, path or flower bed shown with correct size but not necessarily in correct position	B1 <i>Ra</i>	Labels not necessary Patio → 10 cm by 3 cm Vegetable patch → 10 cm by 1 cm Lawn → 10 cm by 8 cm Path → 10 cm by 1 cm Lawn → circle radius 2 cm
	any two of patio, vegetable patch, lawn, path or flower bed shown with correct sizes but not necessarily in correct position	B1 <i>Rb</i>	
	patio, vegetable patch, lawn and path shown with correct sizes and positions	B1 <i>Aa</i>	
	circular flower bed shown within or at edge of lawn – can be any radius	B1 <i>Aa</i>	
	patio, vegetable patch, lawn, path and circular flower bed with correct sizes, in correct position and labelled correctly	B1 <i>la</i>	
<b>Additional Guidance</b>			
Allow freehand attempt at circle for 4 <sup>th</sup> B1 but not 5 <sup>th</sup> B1 Diagram with front and back reversed can score B1B1B0B1B1 Allow 'horizontal vegetable patch' with ends touching fence			

3 (b)	Alternative method 1
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Q	Answer	Mark	Comments
	$15 \times 4.5$ or $67.5$	<i>Ra</i>	
	their $67.5 \div 7.4$ or $[9.1, 9.122]$ or their $67.5 \div 8.6$ or $[7.8, 7.85]$	M1 <i>Rb</i>	
	their $10 \times 128.50$ or $1285$ or their $8 \times 139.75$ or $1118$	M1 <i>la</i>	their 10 must be from their $[9.1, 9.122]$ their 8 must be from their $[7.8, 7.85]$ both must be rounded up to an integer
	their $1285 - 175$	M1 <i>Aa</i>	or $1285 - 175$ or $1118 + 175$
	167 and No or 1110 and 1118 and No or 1293 and 1285 and No	A2 <i>lb lb</i>	A1 167 or 1110 and 1293 or A1ft correct decision for their values (only if 1 <sup>st</sup> and 4 <sup>th</sup> M marks scored)
	<b>Alternative method 2</b>		
	$15 \times 4.5$ or $67.5$	M1 <i>Ra</i>	
	their $67.5 \div 7.4$ or $[9.1, 9.122]$ or their $67.5 \div 8.6$ or $[7.8, 7.85]$	M1 <i>Rb</i>	or $10 \times 7.4$  or $8 \times 8.6$
	their $10 \times 128.50 - 175$ or $1110$	M1 <i>la</i>	their 10 must be from their $[9.1, 9.122]$ their 8 must be from their $[7.8, 7.85]$ both must be rounded up to an integer
	their $1110 \div 8$	M1 <i>Aa</i>	their $1110 \div 139.75$
	$138(.75)$ or $139$ and No	A2 <i>lb lb</i>	A1 $138(.75)$ or $139$ or $7.9(4 \dots)$ A1ft correct conclusion for their values (only if 1 <sup>st</sup> and 4 <sup>th</sup> M marks scored)

3(b)	Additional Guidance	
	<b>Example</b> (common error) $15 \times 4.5 = 67.5$	M1

Q	Answers	Marks	Comments	
	$8.6^2 = 73.96$ and $7.42 = 54.76$	2		M0
	$1 \times 139.75 = 139.75$ and $2 \times 128.50 = 257$ $257 - 139.75 = 117.25$ No			M0 M1 A1ft
	<b>Example</b> (another common error) $15 + 4.5 = 19.5$ $19.5 \div 8.6 = 2.23$ and $19.5 \div 7.4 = 2.64$ $3 \times 139.75 = 419.25$ and $3 \times 128.50 = 385.50$ $419.25 - 385.50 = 33.75$ No			M0 M1 M1 M1 A1ft
	Failing to round up the number of boxes can score M1M1M0M1A1ft			

3 (c)	50 (cm)	B1 Aa		
	$246\ 300 \times \text{their } 50$ or $12\ 315\ 000$	M1 Rb	allow digits 12315	
	their $12\ 315\ 000 \div 1000$ or 12 315	their $12\ 315\ 000 \div 800$ or 15 393.75	M1 Rc	or $800 \times 1000$ or 800 000
	their $12\ 315 \div 800$ or 15.3(9...) or 15.4	their $15\ 393.7 \div 1000$ or 15.3(9...) or 15.4	M1 Aa	or their $12\ 315\ 000 \div 800\ 000$ or 15.3(9...) or 15.4
	16	A1 Ib		
	<b>Additional Guidance</b>			
Multiplying by their 50 can be done at any stage in the calculation				

4 (a)	$2 \times 1 (+) 3 \times 4 (+) 4 \times 9 (+) 5 \times 12$ $(+) 6 \times 12 (+) 7 \times 15 (+) 8 \times 33$ $(+) 9 \times 698 (+) 10 \times 512$ or $2 (+) 12 (+) 36 (+) 60 (+) 72 (+) 105$ $(+) 264 (+) 6282 (+) 5120$	M1 Ra	at least 4 correct
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Q	Answer	Mark	Comments
	$2 \times 1 + 3 \times 4 + 4 \times 9 + 5 \times 12 + 6 \times 12$ $+ 7 \times 15 + 8 \times 33 + 9 \times 698$ $+ 10 \times 512$ or $2 + 12 + 36 + 60 + 72 + 105 + 264 + 6282 + 5120$ or 11 953	M1 Ra	allow two errors
	their 11 953 $\div$ 1296 or [9.2, 9.23]	M1 Rc	
	[92, 92.3]	A1ft Aa	ft their [9.2, 9.23] can be implied from plotted point
	their [92, 92.3] plotted for July $\pm$ $\frac{1}{2}$ small square	B1ft Aa	SC2 correct value plotted with no or incomplete working

4 (b)	Full description e.g. rating increases by about their 11% rating increases (from 81%) to their 92%	B2ft lb lb	B1 Part description e.g. rating increases ft their 4(a)
<b>Additional Guidance</b>			
Mark from answer in 4(a) working space if point not plotted on graph Mark positively if answer in 4(a) working space is incompatible with graph Award B1 for 'rating increases' oe without evidence or with incompatible evidence in 4(a)			

Q	Answer	Mark	Comments
4 (c)	<b>Alternative method 1</b>		
	678 + 411 or 1089 or 12 + 18 + 56 + 54 or 140	M1 Ra	happy and unhappy customers
	their 1089 ÷ 1296 (× 100) or 0.84 or 84.0 or their 140 ÷ 1296 (× 100) or [0.108, 0.109] or [10.8, 10.9]	M1 Aa	
	73.2 or 73 and No or 0.732 or 0.73 and 0.75 and No	A2 lb	A1 73.2 or 73 or 0.732 or 0.73 and 0.75 or A1ft correct conclusion for their values (only if M2 scored)
	<b>Alternative method 2</b>		
	1296 ÷ 100 × 75 or 972	M1 Aa	
	(678 + 411) – (12 + 18 + 56 + 54) or 1089 – 140 or 949	M1 Ra	
	972 and 949 and No	A2 lb	A1 972 and 949 or A1ft correct conclusion for their values (only if M2 scored)

4(c)	<b>Alternative method 3</b>
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Q	Answer	Mark	Comments
	678 + 411 or 1089 or 12 + 18 + 56 + 54 or 140	M1 Ra	happy and unhappy customers
	(their 1089 – their 140) ÷ 1296 (× 100) or 949 ÷ 1296 (× 100) or 0.732 or 0.73	M1 Ra	
	73.2 or 73 and No or 0.732 or 0.73 and 0.75 and No	A2 lb	A1 73.2 or 73 or 0.732 or 0.73 and 0.75 or A1ft correct conclusion for their values (only if M2 scored)

Additional Guidance		
4(c)	<b>Example</b> (common error - rounding 10.8% down to 10) 1089 and 140 0.84 = 84% and 0.108 = 10% 74% and No	M1 M1 A1ft
	Any answer that does not include the conversion to or from a % → M1 max	

4 (d)	<b>Alternative method 1</b>		
	55 ÷ 100 × 1128 or 620(.4)	M1 Ra	

Q	Answer	Mark	Comments
	620(.4) and No	A1 <i>lb</i>	
	<b>Alternative method 2</b>		
	$615 \div 1128 (\times 100)$	M1 <i>Ra</i>	
	54(.5 ...) and No	A1 <i>lb</i>	
	<b>Alternative method 3</b>		
	$615 \div (55 \div 100)$ or 1118 ...	M1 <i>Ra</i>	
	1118 ... and No	A1 <i>lb</i>	