



A-level

Physics data and formulae

For use in exams from the June 2017 Series onwards

[Turn over]

DATA - FUNDAMENTAL CONSTANTS AND VALUES

Quantity	Symbol	Value	Units
speed of light in vacuo	c	3.00×10^8	m s^{-1}
permeability of free space	μ_0	$4\pi \times 10^{-7}$	H m^{-1}
permittivity of free space	ϵ_0	8.85×10^{-12}	F m^{-1}
magnitude of the charge of electron	e	1.60×10^{-19}	C
the Planck constant	h	6.63×10^{-34}	J s
gravitational constant	G	6.67×10^{-11}	$\text{N m}^2 \text{kg}^{-2}$
the Avogadro constant	N_A	6.02×10^{23}	mol^{-1}
molar gas constant	R	8.31	$\text{J K}^{-1} \text{mol}^{-1}$
the Boltzmann constant	k	1.38×10^{-23}	J K^{-1}
the Stefan constant	σ	5.67×10^{-8}	$\text{W m}^{-2} \text{K}^{-4}$
the Wien constant	α	2.90×10^{-3}	m K
electron rest mass (equivalent to 5.5×10^{-4} u)	m_e	9.11×10^{-31}	kg

electron charge/mass ratio	$\frac{e}{m_e}$	1.76×10^{11}	C kg ⁻¹
proton rest mass (equivalent to 1.00728 u)	m_p	$1.67(3) \times 10^{-27}$	kg
proton charge/mass ratio	$\frac{e}{m_p}$	9.58×10^7	C kg ⁻¹
neutron rest mass (equivalent to 1.00867 u)	m_n	$1.67(5) \times 10^{-27}$	kg
gravitational field strength	g	9.81	N kg ⁻¹
acceleration due to gravity	g	9.81	m s ⁻²
atomic mass unit (1u is equivalent to 931.5 MeV)	u	1.661×10^{-27}	kg

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ALGEBRAIC EQUATION

quadratic equation $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

ASTRONOMICAL DATA

Body	Mass/kg	Mean radius/m
Sun	1.99×10^{30}	6.96×10^8
Earth	5.97×10^{24}	6.37×10^6

GEOMETRICAL EQUATIONS

arc length $= r\theta$

circumference of circle $= 2\pi r$

area of circle $= \pi r^2$

curved surface area of cylinder $= 2\pi rh$

area of sphere $= 4\pi r^2$

volume of sphere $= \frac{4}{3} \pi r^3$

PARTICLE PHYSICS

Class	Name	Symbol	Rest energy/MeV
photon	photon	γ	0
lepton	neutrino	ν_e	0
		ν_μ	0
	electron	e^\pm	0.510999
	muon	μ^\pm	105.659
mesons	π meson	π^\pm	139.576
		π^0	134.972
	K meson	K^\pm	493.821
		K^0	497.762
baryons	proton	p	938.257
	neutron	n	939.551

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PROPERTIES OF QUARKS antiquarks have opposite signs

Type	Charge	Baryon number	Strangeness
u	$+\frac{2}{3}e$	$+\frac{1}{3}$	0
d	$-\frac{1}{3}e$	$+\frac{1}{3}$	0
s	$-\frac{1}{3}e$	$+\frac{1}{3}$	-1

PROPERTIES OF LEPTONS

		Lepton number
Particles:	$e^-, \nu_e; \mu^-, \nu_\mu$	+ 1
Antiparticles:	$e^+, \bar{\nu}_e, \mu^+, \bar{\nu}_\mu$	- 1

PHOTONS AND ENERGY LEVELS

photon energy	$E = hf = \frac{hc}{\lambda}$
photoelectricity	$hf = \phi + E_{k(\max)}$
energy levels	$hf = E_1 - E_2$
de Broglie wavelength	$\lambda = \frac{h}{p} = \frac{h}{mv}$

[Turn over]

WAVES

wave speed	$c = f\lambda$	period	$f = \frac{1}{T}$
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first harmonic	$f = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$
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fringe spacing	$w = \frac{\lambda D}{s}$	diffraction grating	$d \sin \theta = n\lambda$
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refractive index of a substance s , $n = \frac{c}{c_s}$

for two different substances of refractive indices n_1 and n_2 ,

law of refraction $n_1 \sin \theta_1 = n_2 \sin \theta_2$

critical angle $\sin \theta_c = \frac{n_2}{n_1}$ for $n_1 > n_2$

MECHANICS

moments

$$\text{moment} = Fd$$

**velocity and
acceleration**

$$v = \frac{\Delta s}{\Delta t}$$

$$a = \frac{\Delta v}{\Delta t}$$

**equations of
motion**

$$v = u + at$$

$$s = \left(\frac{u + v}{2} \right) t$$

$$v^2 = u^2 + 2as$$

$$s = ut + \frac{at^2}{2}$$

force

$$F = ma$$

force

$$F = \frac{\Delta(mv)}{\Delta t}$$

impulse

$$F \Delta t = \Delta(mv)$$

**work, energy
and power**

$$W = F s \cos \theta$$

$$E_k = \frac{1}{2} m v^2$$

$$\Delta E_p = mg\Delta h$$

$$P = \frac{\Delta W}{\Delta t}, P = Fv$$

$$\text{efficiency} = \frac{\text{useful output power}}{\text{input power}}$$

[Turn over]

MATERIALS

density $\rho = \frac{m}{v}$

Hooke's law $F = k \Delta L$

Young modulus $= \frac{\text{tensile stress}}{\text{tensile strain}}$

tensile stress $= \frac{F}{A}$

tensile strain $= \frac{\Delta L}{L}$

energy stored $E = \frac{1}{2} F \Delta L$

ELECTRICITY

current and pd $I = \frac{\Delta Q}{\Delta t} \quad V = \frac{W}{Q} \quad R = \frac{V}{I}$

resistivity $\rho = \frac{RA}{L}$

resistors in series $R_T = R_1 + R_2 + R_3 + \dots$

resistors in parallel $\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$

power $P = VI = I^2 R = \frac{V^2}{R}$

emf $\varepsilon = \frac{E}{Q} \quad \varepsilon = I(R + r)$

CIRCULAR MOTION**magnitude of
angular speed**

$$\omega = \frac{v}{r}$$

$$\omega = 2\pi f$$

**centripetal
acceleration**

$$a = \frac{v^2}{r} = \omega^2 r$$

**centripetal
force**

$$F = \frac{mv^2}{r} = m\omega^2 r$$

SIMPLE HARMONIC MOTION**acceleration**

$$a = -\omega^2 x$$

displacement

$$x = A \cos(\omega t)$$

speed

$$v = \pm \omega \sqrt{(A^2 - x^2)}$$

maximum speed

$$v_{\max} = \omega A$$

maximum acceleration

$$a_{\max} = \omega^2 A$$

for a mass-spring system

$$T = 2\pi \sqrt{\frac{m}{k}}$$

for a simple pendulum

$$T = 2\pi \sqrt{\frac{l}{g}}$$

[Turn over]

THERMAL PHYSICS

energy to change
temperature

$$Q = mc\Delta\theta$$

energy to change
state

$$Q = ml$$

gas law

$$pV = nRT$$

$$pV = NkT$$

kinetic theory
model

$$pV = \frac{1}{3}Nm(c_{\text{rms}})^2$$

kinetic energy of
gas molecule

$$\frac{1}{2}m(c_{\text{rms}})^2 = \frac{3}{2}kT = \frac{3RT}{2N_A}$$

GRAVITATIONAL FIELDS

force between two
masses

$$F = \frac{Gm_1m_2}{r^2}$$

gravitational field
strength

$$g = \frac{F}{m}$$

magnitude of
gravitational field
strength in a radial
field

$$g = \frac{GM}{r^2}$$

work done

$$\Delta W = m\Delta V$$

gravitational
potential

$$V = -\frac{GM}{r}$$

$$g = -\frac{\Delta V}{\Delta r}$$

ELECTRIC FIELDS AND CAPACITORS

force between
two point
charges

$$F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}$$

force on a charge

$$F = EQ$$

field strength for
a uniform field

$$E = \frac{V}{d}$$

work done

$$\Delta W = Q\Delta V$$

field strength for
a radial field

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$$

electric potential

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

field strength

$$E = \frac{\Delta V}{\Delta r}$$

capacitance

$$C = \frac{Q}{V}$$

$$C = \frac{A\epsilon_0\epsilon_r}{d}$$

capacitor energy
stored

$$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2} \frac{Q^2}{C}$$

[Turn over]

capacitor charging $Q = Q_0(1 - e^{-\frac{t}{RC}})$

decay of charge $Q = Q_0 e^{-\frac{t}{RC}}$

time constant RC

MAGNETIC FIELDS

force on a current $F = BIl$

force on a moving charge $F = BQv$

magnetic flux $\Phi = BA$

magnetic flux linkage $N\Phi = BAN \cos \theta$

magnitude of induced emf $\varepsilon = N \frac{\Delta\Phi}{\Delta t}$

$$N\Phi = BAN \cos \theta$$

emf induced in a rotating coil $\varepsilon = BAN\omega \sin \omega t$

alternating current $I_{\text{rms}} = \frac{I_0}{\sqrt{2}} \quad V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$

transformer equations $\frac{N_s}{N_p} = \frac{V_s}{V_p}$

$$\text{efficiency} = \frac{I_s V_s}{I_p V_p}$$

NUCLEAR PHYSICS

inverse square law
for γ radiation

$$I = \frac{k}{x^2}$$

radioactive decay

$$\frac{\Delta N}{\Delta t} = -\lambda N, N = N_0 e^{-\lambda t}$$

activity

$$A = \lambda N$$

half-life

$$T_{1/2} = \frac{\ln 2}{\lambda}$$

nuclear radius

$$R = R_0 A^{1/3}$$

energy-mass
equation

$$E = mc^2$$

[Turn over]

OPTIONS

ASTROPHYSICS

1 astronomical unit = 1.50×10^{11} m

1 light year = 9.46×10^{15} m

1 parsec = 2.06×10^5 AU = 3.08×10^{16} m = 3.26 ly

Hubble constant, $H = 65 \text{ km s}^{-1} \text{ Mpc}^{-1}$

$$M = \frac{\text{angle subtended by image at eye}}{\text{angle subtended by object at unaided eye}}$$

telescope in normal adjustment $M = \frac{f_o}{f_e}$

Rayleigh criterion $\theta \approx \frac{\lambda}{D}$

magnitude equation $m - M = 5 \log \frac{d}{10}$

Wien's law $\lambda_{\text{max}} T = 2.9 \times 10^{-3} \text{ m K}$

Stefan's law $P = \sigma AT^4$

Schwarzschild radius $R_s \approx \frac{2GM}{c^2}$

Doppler shift for $v \ll c$ $\frac{\Delta f}{f} = - \frac{\Delta \lambda}{\lambda} = \frac{v}{c}$

red shift $z = - \frac{v}{c}$

Hubble's law $v = Hd$

[Turn over]

MEDICAL PHYSICS

lens equations $P = \frac{1}{f}$

$$m = \frac{v}{u}$$

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$$

threshold of hearing $I_0 = 1.0 \times 10^{-12} \text{ W m}^{-2}$

intensity level $\text{intensity level} = 10 \log \frac{I}{I_0}$

absorption $I = I_0 e^{-\mu x}$

$$\mu_m = \frac{\mu}{\rho}$$

ultrasound imaging $Z = p c$

$$\frac{I_r}{I_i} = \left(\frac{Z_2 - Z_1}{Z_2 + Z_1} \right)^2$$

half-lives $\frac{1}{T_E} = \frac{1}{T_B} + \frac{1}{T_P}$

ENGINEERING PHYSICS

moment of inertia $I = \Sigma mr^2$

angular kinetic energy $E_k = \frac{1}{2} I\omega^2$

equations of angular motion $\omega_2 = \omega_1 + \alpha t$

$$\omega_2^2 = \omega_1^2 + 2\alpha\theta$$

$$\theta = \omega_1 t + \frac{\alpha t^2}{2}$$

$$\theta = \frac{(\omega_1 + \omega_2) t}{2}$$

torque $T = I \alpha$

$$T = F r$$

angular momentum angular momentum = $I \omega$

angular impulse $T\Delta t = \Delta(I\omega)$

work done $W = T\theta$

power $P = T\omega$

thermodynamics $Q = \Delta U + W$

$$W = p\Delta V$$

adiabatic change $pV^\gamma = \text{constant}$

isothermal change $pV = \text{constant}$

[Turn over]

heat engines

$$\text{efficiency} = \frac{W}{Q_H} = \frac{Q_H - Q_C}{Q_H}$$

$$\text{maximum theoretical efficiency} = \frac{T_H - T_C}{T_H}$$

work done per cycle = area of loop

input power = calorific value × fuel flow rate

**indicated power = (area of $p - V$ loop)
 × (number of cycles per second)
 × (number of cylinders)**

output or brake power $P = T\omega$

friction power = indicated power — brake power

heat pumps and refrigerators

$$\text{refrigerator: } COP_{\text{ref}} = \frac{Q_C}{W} = \frac{Q_C}{Q_H - Q_C}$$

$$\text{heat pump: } COP_{\text{hp}} = \frac{Q_H}{W} = \frac{Q_H}{Q_H - Q_C}$$

TURNING POINTS IN PHYSICS

electrons in fields

$$F = \frac{eV}{d}$$

$$F = Bev$$

$$r = \frac{mv}{Be}$$

$$\frac{1}{2}mv^2 = eV$$

Millikan's
experiment

$$\frac{QV}{d} = mg$$

$$F = 6\pi\eta rv$$

Maxwell's formula

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2meV}}$$

[Turn over]

special relativity

$$t = \frac{t_0}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$l = l_0 \sqrt{1 - \frac{v^2}{c^2}}$$

$$E = mc^2 = \frac{m_0 c^2}{\sqrt{1 - \frac{v^2}{c^2}}}$$

ELECTRONICS**resonant
frequency**

$$f_0 = \frac{1}{2\pi \sqrt{LC}}$$

Q-factor

$$Q = \frac{f_0}{f_B}$$

**operational
amplifiers: open
loop**

$$V_{\text{out}} = A_{\text{OL}} (V_+ - V_-)$$

inverting amplifier

$$\frac{V_{\text{out}}}{V_{\text{in}}} = - \frac{R_f}{R_{\text{in}}}$$

**non-inverting
amplifier**

$$\frac{V_{\text{out}}}{V_{\text{in}}} = 1 + \frac{R_f}{R_1}$$

**summing
amplifier**

$$V_{\text{out}} = -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} + \dots \right)$$

difference amplifier

$$V_{\text{out}} = (V_+ - V_-) \frac{R_f}{R_1}$$

Bandwidth requirement:

for AM bandwidth = $2f_M$

for FM bandwidth = $2(\Delta f + f_M)$

END OF FORMULAE

There are no formulae printed on this page

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