



**Surname** \_\_\_\_\_

**Other Names** \_\_\_\_\_

**Centre Number** \_\_\_\_\_

**Candidate Number** \_\_\_\_\_

**Candidate Signature** \_\_\_\_\_

**A-level  
MATHEMATICS**

**Paper 3**

**7357/3**

**Friday 14 June 2019 Afternoon**

**Time allowed: 2 hours**

**At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.**

**[Turn over]**



**For this paper you must have:**

- **an AQA Formulae for A-level Mathematics booklet.**
- **a graphical or scientific calculator that meets the requirements of the specification.**

## **INSTRUCTIONS**

- **Use black ink or black ball-point pen. Pencil should only be used for drawing.**
- **Answer ALL questions.**
- **You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do NOT use the space provided for a different question.**
- **Show all necessary working; otherwise marks for method may be lost.**
- **Do all rough work in this book. Cross through any work that you do not want to be marked.**



## **INFORMATION**

- **The marks for questions are shown in brackets.**
- **The maximum mark for this paper is 100.**

## **ADVICE**

- **Unless stated otherwise, you may quote formulae, without proof, from the booklet.**
- **You do not necessarily need to use all the space provided.**

**DO NOT TURN OVER UNTIL TOLD TO DO SO**



## SECTION A

Answer ALL questions in the spaces provided.

1  $f(x) = \arcsin x$

State the maximum possible domain of  $f$

Tick (✓) ONE box. [1 mark]

$\{x \in \mathbb{R} : -1 \leq x \leq 1\}$

$\left\{x \in \mathbb{R} : -\frac{\pi}{2} \leq x \leq \frac{\pi}{2}\right\}$

$\{x \in \mathbb{R} : -\pi \leq x \leq \pi\}$

$\{x \in \mathbb{R} : -90 \leq x \leq 90\}$

2 Find the value of  $\frac{100!}{98! \times 3!}$

Circle your answer. [1 mark]

$$\frac{50}{147}$$

1650

3300

161 700

3 Given  $u_1 = 1$ , determine which one of the formulae below defines an increasing sequence for  $n \geq 1$

Circle your answer. [1 mark]

$$u_{n+1} = 1 + \frac{1}{u_n}$$

$$u_n = 2 - 0.9^{n-1}$$

$$u_{n+1} = -1 + 0.5u_n$$

$$u_n = 0.9^{n-1}$$

[Turn over]



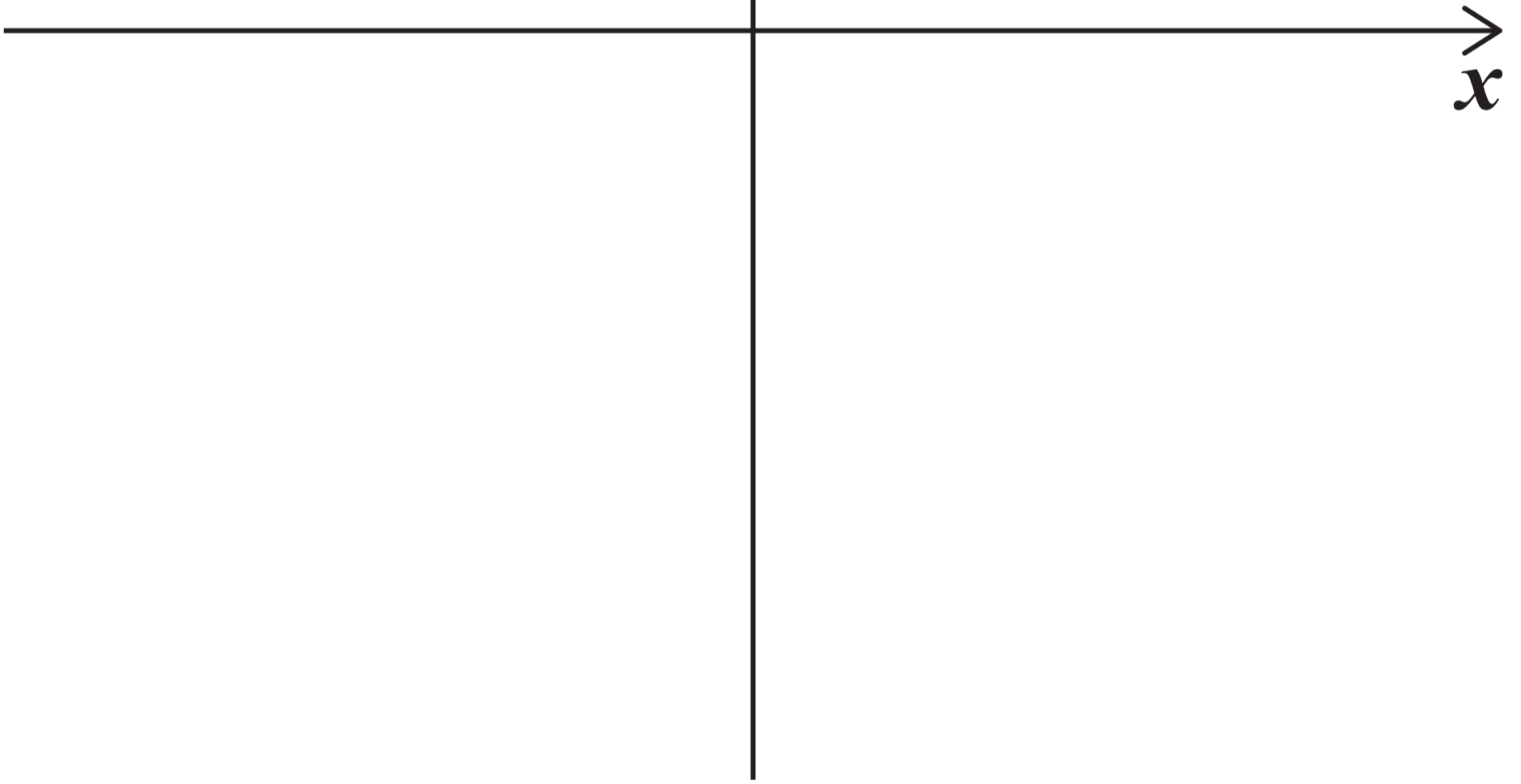
**4** On page 7 sketch the region defined by the inequalities

$$y \leq (1 - 2x)(x + 3) \text{ and } y - x \leq 3$$

**Clearly indicate your region by shading it in and labelling it  $R$ .  
[3 marks]**

7

$y$   $\uparrow$



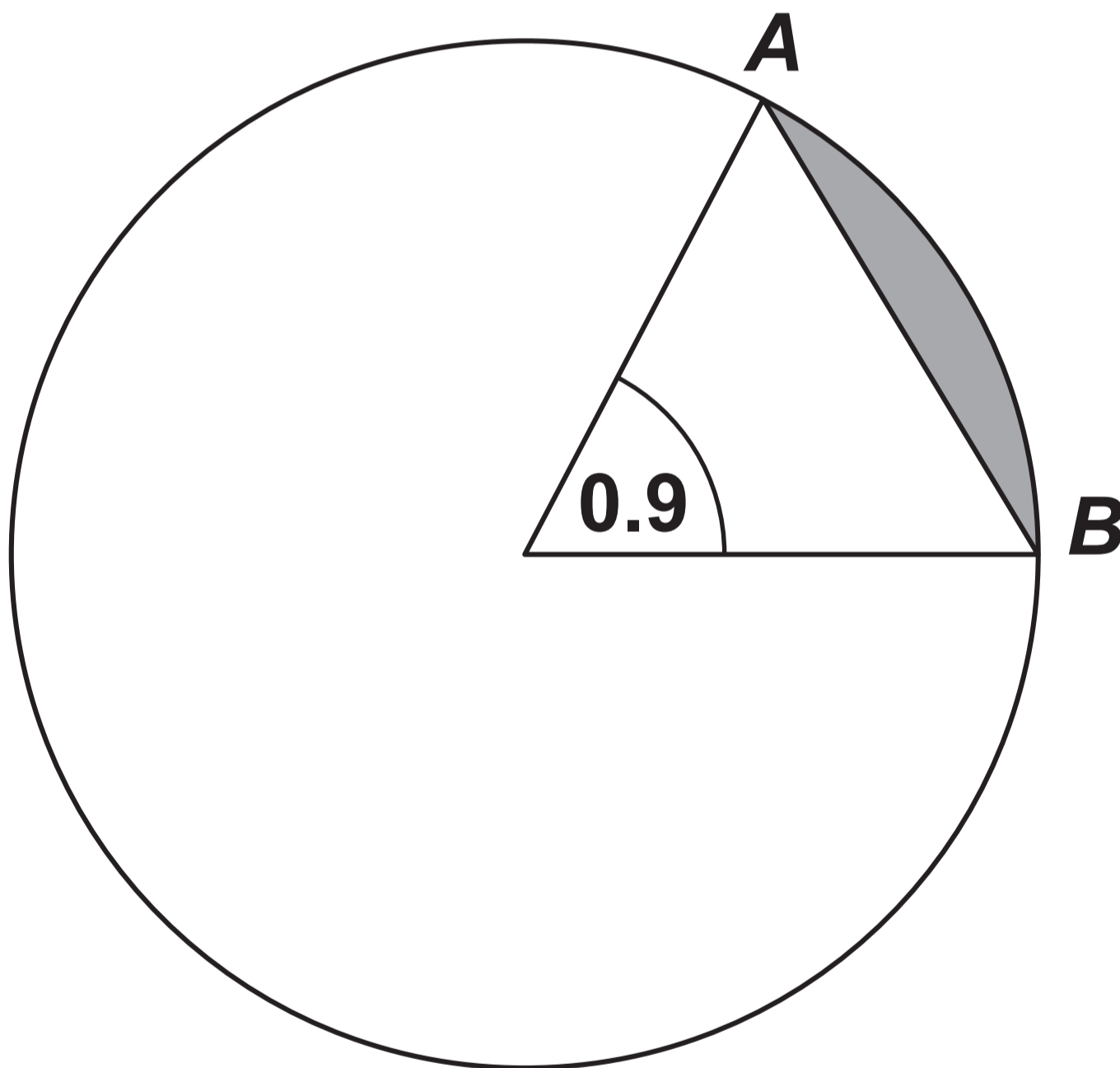
**[Turn over]**



5 A circle has equation  
 $x^2 + y^2 - 6x - 8y = 264$

$AB$  is a chord of the circle.

The angle at the centre of the circle, subtended by  $AB$ , is 0.9 radians, as shown in the diagram below.



Find the area of the minor segment shaded on the diagram.

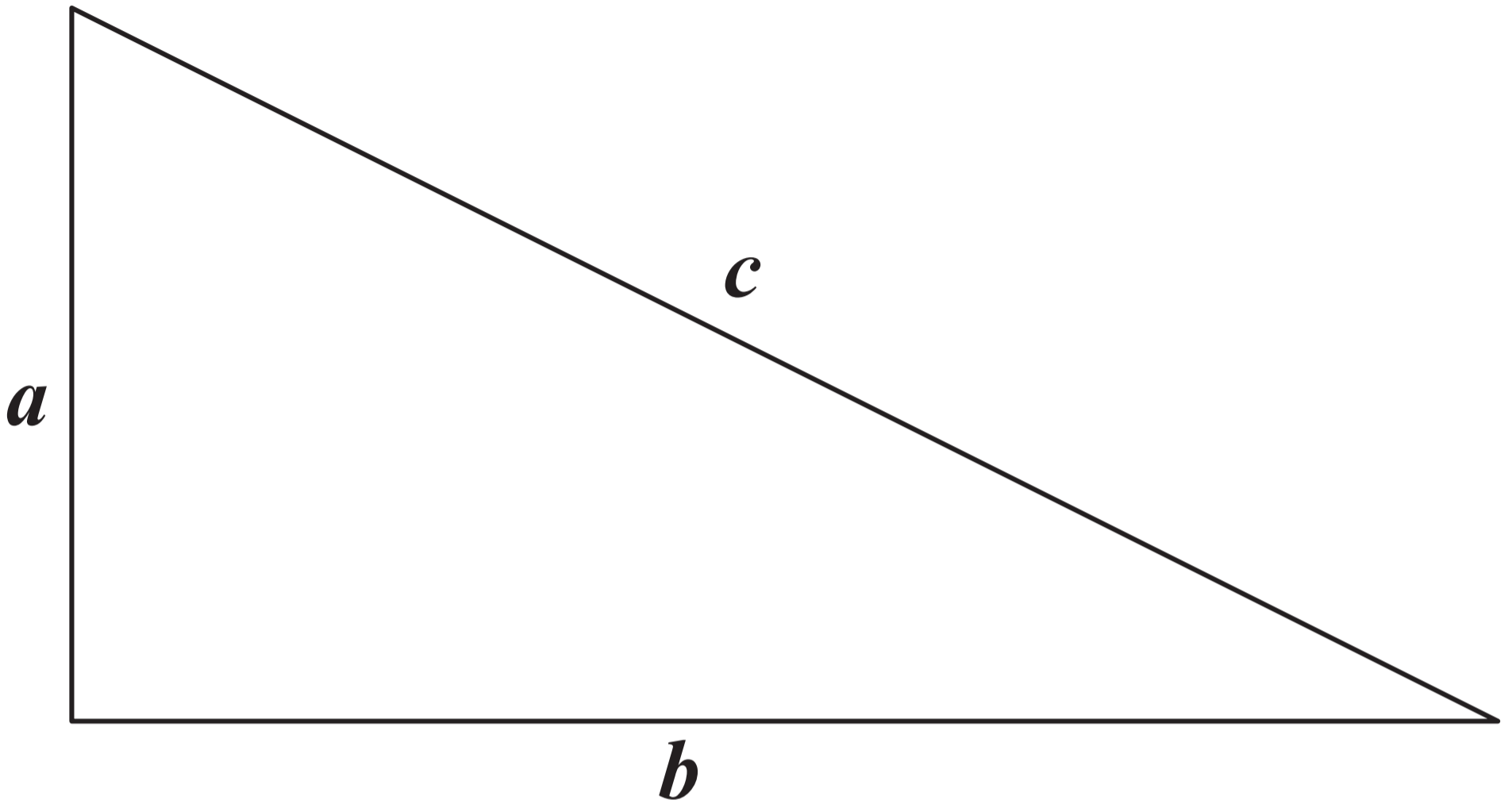
Give your answer to three significant figures. [5 marks]







- 6 The three sides of a right-angled triangle have lengths  $a$ ,  $b$  and  $c$ , where  $a, b, c \in \mathbb{Z}$



- 6 (a) State an example where  $a$ ,  $b$  and  $c$  are all even. [1 mark]

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[Turn over]





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**[Turn over]**





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**[Turn over]**









**8** A student is conducting an experiment in a laboratory to investigate how quickly liquids cool to room temperature.

A beaker containing a hot liquid at an initial temperature of  $75^{\circ}\text{C}$  cools so that the temperature,  $\theta^{\circ}\text{C}$ , of the liquid at time  $t$  minutes can be modelled by the equation

$$\theta = 5(4 + \lambda e^{-kt})$$

where  $\lambda$  and  $k$  are constants.

After 2 minutes the temperature falls to  $68^{\circ}\text{C}$ .

**8 (a)** Find the temperature of the liquid after 15 minutes.

Give your answer to three significant figures. [7 marks]

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**8 (c) Explain why the model might need to be changed if the experiment was conducted in a different place. [1 mark]**

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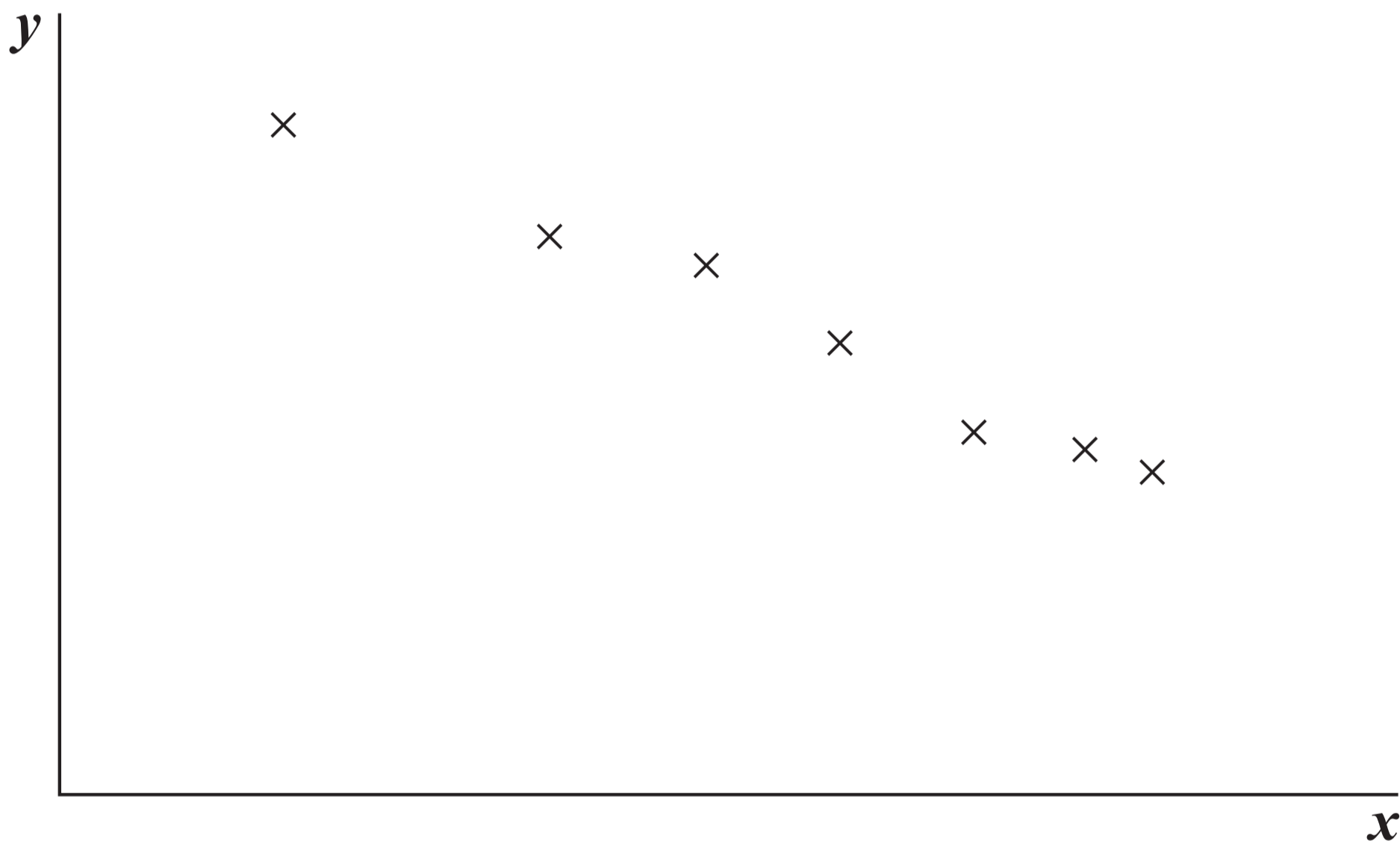
**[Turn over]**



## SECTION B

Answer ALL questions in the spaces provided.

- 10 Which of the options best describes the correlation shown in the diagram below?





**33**

**Tick (✓) ONE box. [1 mark]**

**moderate positive**

**strong positive**

**moderate negative**

**strong negative**

**[Turn over]**



**11 Lenny is one of a team of people interviewing shoppers in a town centre.**

**He is asked to survey 50 women between the ages of 18 and 29**

**Identify the name of this type of sampling.**

**Circle your answer. [1 mark]**

**simple      stratified      quota      systematic**  
**random**

**12 Amelia decides to analyse the heights of members of her school rowing club.**

**The heights of a random sample of 10 rowers are shown in the table on page 36.**

**[Turn over]**





<b>ROWER</b>	<b>Jess</b>	<b>Nell</b>	<b>Liv</b>	<b>Neve</b>	<b>Ann</b>	<b>Tori</b>	<b>Maya</b>	<b>Kath</b>	<b>Darcy</b>	<b>Jen</b>
<b>HEIGHT (cm)</b>	<b>162</b>	<b>169</b>	<b>172</b>	<b>156</b>	<b>146</b>	<b>161</b>	<b>159</b>	<b>164</b>	<b>157</b>	<b>160</b>

**12 (a) Any value more than 2 standard deviations from the mean may be regarded as an outlier.**

**Verify that Ann's height is an outlier.**

**Fully justify your answer. [4 marks]**

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**[Turn over for the next question]**



**13** Patrick is practising his skateboarding skills. On each day, he has 30 attempts at performing a difficult trick.

Every time he attempts the trick, there is a probability of 0.2 that he will fall off his skateboard.

Assume that the number of times he falls off on any given day may be modelled by a binomial distribution.

**13(a)(i)** Find the mean number of times he falls off in a day. [1 mark]

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**13(a)(ii) Find the variance of the number of times he falls off in a day.  
[1 mark]**

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**[Turn over]**





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**13 (c) Patrick has 30 attempts to perform the trick on each of 5 consecutive days.**



**13(c) (i) Calculate the probability that he will fall off his skateboard at least 5 times on each of the 5 days.  
[2 marks]**

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**[Turn over]**

**13(c)(ii) Explain why it may be unrealistic to use the same value of 0.2 for the probability of falling off for all 5 days. [1 mark]**

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**[Turn over for the next question]**





**A survey was conducted into the health of 120 teachers.**

**The survey recorded whether or not they had suffered from a range of four health issues in the past year.**

**In addition, their physical exercise level was categorised as low, medium or high.**

48

**50 teachers had a low exercise level, 40 teachers had a medium exercise level and 30 teachers had a high exercise level.**

**The results of the survey are shown in the table on page 49.**





	<b>LOW EXERCISE</b>	<b>MEDIUM EXERCISE</b>	<b>HIGH EXERCISE</b>
<b>BACK TROUBLE</b>	14	7	10
<b>STRESS</b>	38	14	5
<b>DEPRESSION</b>	9	2	1
<b>HEADACHE/ MIGRAINE</b>	4	5	5

**[Turn over]**

**14 (a) Find the probability that a randomly selected teacher:**

**14(a) (i) suffers from back trouble and has a high exercise level; [1 mark]**

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**15 Jamal, a farmer, claims that the larger the rainfall, the greater the yield of wheat from his farm.**

**He decides to investigate his claim, at the 5% level of significance.**

**He measures the rainfall in centimetres and the yield in kilograms for a random sample of ten years.**

**He correctly calculates the product moment correlation coefficient between rainfall and yield for his sample to be 0.567**

The table below shows the critical values for correlation coefficients for a sample size of 10 for different significance levels, for both 1- and 2-tailed tests.

<b>1-TAILED TEST SIGNIFICANCE LEVEL</b>	<b>5%</b>	<b>2.5%</b>	<b>1%</b>	<b>0.5%</b>
<b>2-TAILED TEST SIGNIFICANCE LEVEL</b>	<b>10%</b>	<b>5%</b>	<b>2%</b>	<b>1%</b>
<b>CRITICAL VALUE</b>	<b>0.549</b>	<b>0.632</b>	<b>0.716</b>	<b>0.765</b>

[Turn over]







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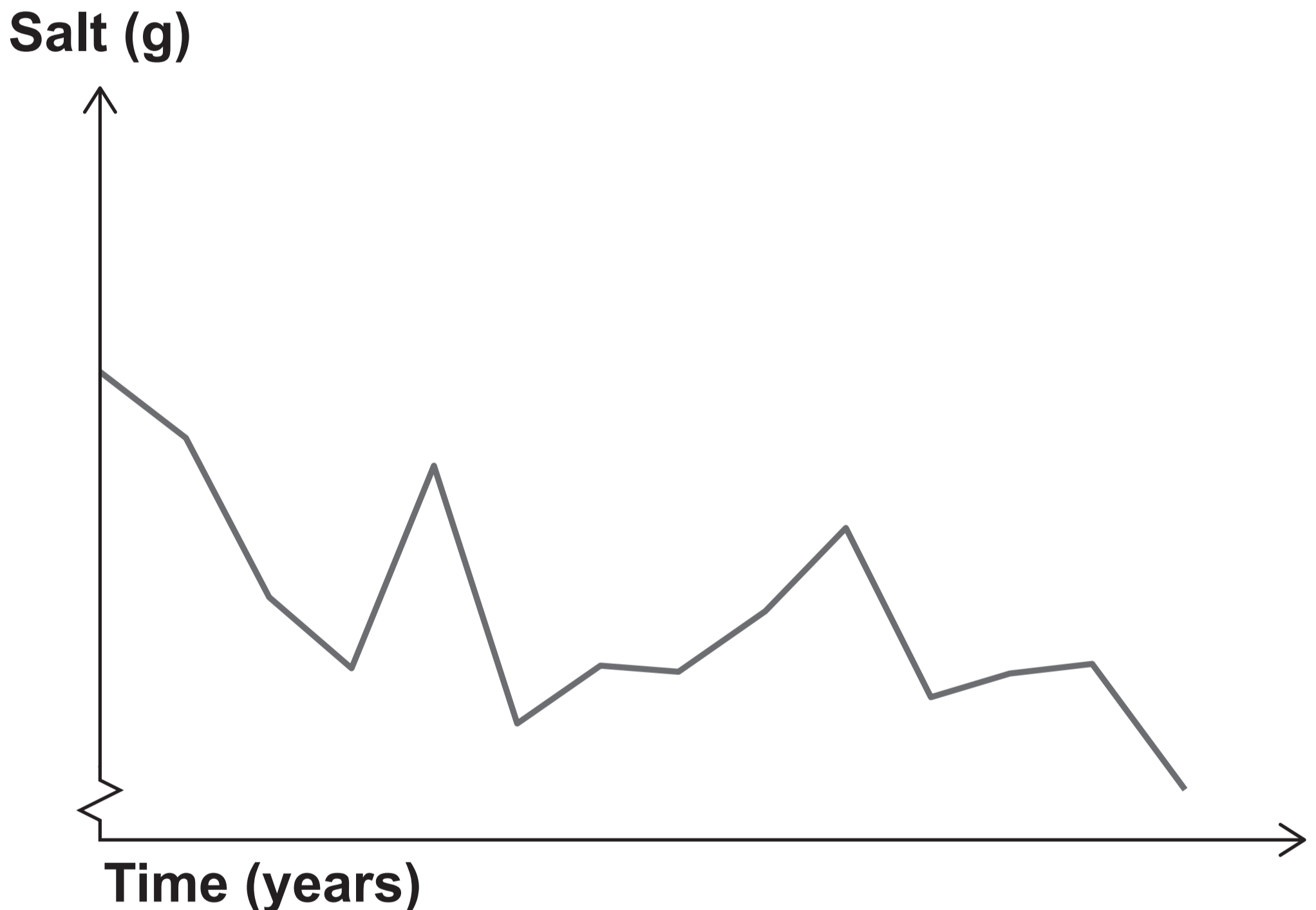
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**[Turn over]**



- 16 (a)** The graph below shows the amount of salt, in grams, purchased per person per week in England between 2001–02 and 2014, based upon the Large Data Set.



**Meera and Gemma are arguing about what this graph shows.**

**Meera believes that the amount of salt consumed by people decreased greatly during this period.**





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**16 (b) It is known that the mean amount of sugar purchased per person in England in 2014 was 78.9 grams, with a standard deviation of 25.0 grams.**

**In 2018, a sample of 918 people had a mean of 80.4 grams of sugar purchased per person.**

**Investigate, at the 5% level of significance, whether the mean amount of sugar purchased per person in England has changed between 2014 and 2018.**

**Assume that the survey data is a random sample taken from a normal distribution and that the standard deviation has remained the same. [6 marks]**

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**[Turn over]**







**16 (c) Another test is performed to determine whether the mean amount of fat purchased per person has changed between 2014 and 2018.**

**At the 10% significance level, the null hypothesis is rejected.**

**With reference to the 10% significance level, explain why it is not necessarily true that there has been a change. [2 marks]**

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**[Turn over]**



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**17 Elizabeth's Bakery makes brownies.**

**It is known that the mass,  $X$  grams, of a brownie may be modelled by a normal distribution.**

**10% of the brownies have a mass less than 30 grams.**

**80% of the brownies have a mass greater than 32.5 grams.**

**17 (a) Find the mean and standard deviation of  $X$ . [7 marks]**

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**[Turn over]**







**17(b)(i) Find  $P(X \neq 35)$  [1 mark]**

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**17(b)(ii) Find  $P(X < 35)$  [2 marks]**

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**[Turn over]**



**17 (c) Brownies are baked in batches of 13.**

**Calculate the probability that, in a batch of brownies, no more than 3 brownies are less than 35 grams.**

**You may assume that the masses of brownies are independent of each other. [2 marks]**

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**[Turn over]**





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**END OF QUESTIONS**



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For Examiner's Use	
Question	Mark
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<b>TOTAL</b>	

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