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Other Names \_\_\_\_\_

Centre Number \_\_\_\_\_

Candidate Number \_\_\_\_\_

Candidate Signature \_\_\_\_\_

I declare this is my own work.

# A-level FURTHER MATHEMATICS

Paper 1

**7367/1**

Friday 22 May 2020 Morning

Time allowed: 2 hours

**You must have:**

- the AQA formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)

At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.

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**INSTRUCTIONS**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Answer ALL questions.
- You must answer each question in the space provided for that question.
- Do NOT write on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

**INFORMATION**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

**ADVICE**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

**DO NOT TURN OVER UNTIL TOLD TO DO SO**



Answer ALL questions in the space provided.

- 1 Which of the integrals below is NOT an improper integral?

Circle your answer. [1 mark]

$$\int_0^{\infty} e^{-x} dx$$

$$\int_0^2 \frac{1}{1-x^2} dx$$

$$\int_0^1 \sqrt{x} dx$$

$$\int_0^1 \frac{1}{\sqrt{x}} dx$$



- 2 Which one of the matrices below represents a rotation of  $90^\circ$  about the  $x$ -axis?

Circle your answer. [1 mark]

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{bmatrix}$$

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3

The quadratic equation

$ax^2 + bx + c = 0$  ( $a, b, c \in \mathbb{R}$ ) has real roots  $\alpha$  and  $\beta$ .

One of the four statements below is incorrect.

Which statement is INCORRECT?

Tick (✓) ONE box. [1 mark]

$$c = 0 \Rightarrow \alpha = 0 \text{ or } \beta = 0$$

$$c = a \Rightarrow \alpha \text{ is the reciprocal of } \beta$$

$$b < 0 \text{ and } c < 0 \Rightarrow \alpha > 0 \text{ and } \beta > 0$$

$$b = 0 \Rightarrow \alpha = -\beta$$









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**4 (b) Find the value of  $p$  and the value of  $r$ .  
[2 marks]**

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6 Let  $w$  be the root of the equation  $z^7 = 1$  that has the smallest argument  $\alpha$  in the interval  $0 < \alpha < \pi$

6 (a) Prove that  $w^n$  is also a root of the equation  $z^7 = 1$  for any integer  $n$ . [1 mark]

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6 (b) Prove that  $1 + w + w^2 + w^3 + w^4 + w^5 + w^6 = 0$   
[2 marks]

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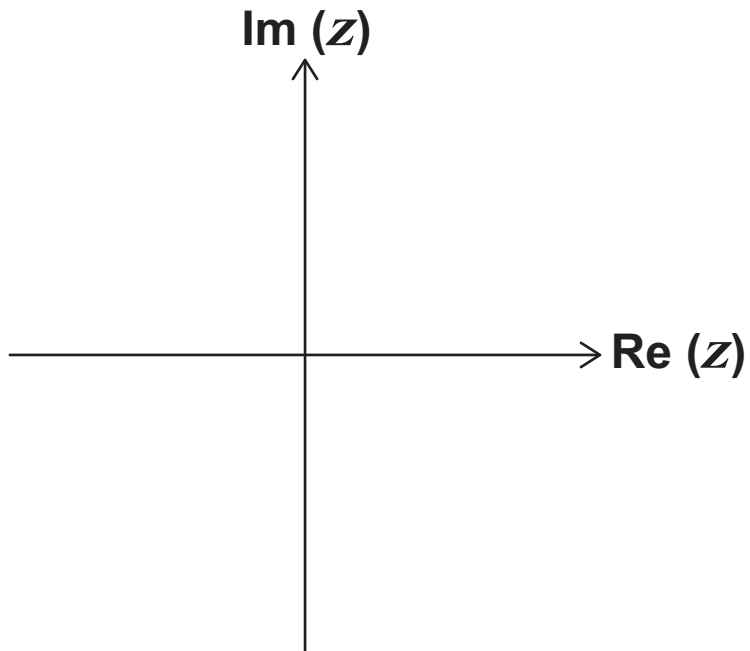
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- 6 (c) Show the positions of  $w$ ,  $w^2$ ,  $w^3$ ,  $w^4$ ,  $w^5$ , and  $w^6$  on the Argand diagram below. [2 marks]







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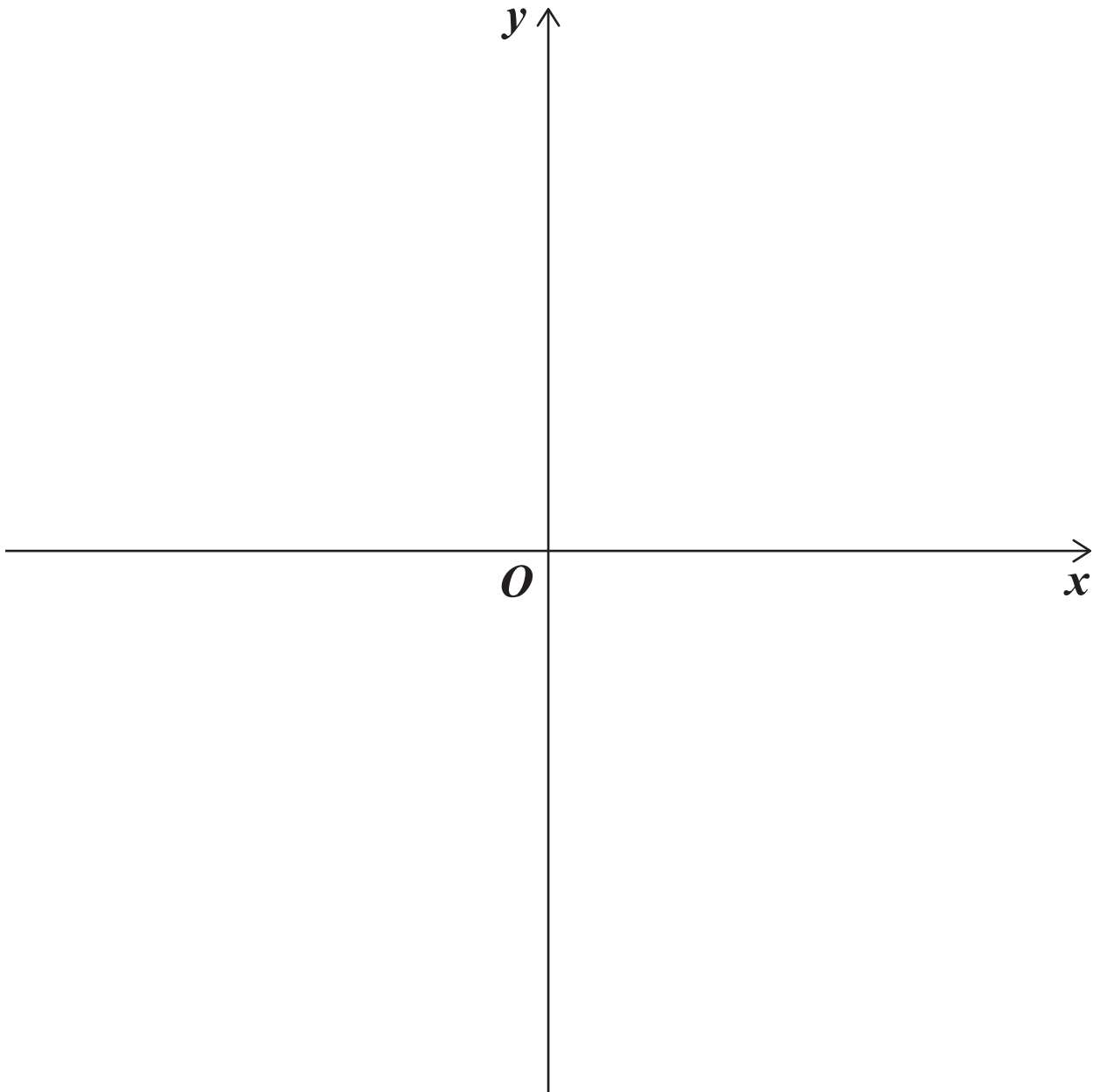
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- 9 (d) Sketch the graph of  $y = f(x)$  on the axes below.  
[4 marks]



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11

The lines  $l_1$ ,  $l_2$  and  $l_3$  are defined as follows.

$$l_1 : \left( r - \begin{bmatrix} 1 \\ 5 \\ -1 \end{bmatrix} \right) \times \begin{bmatrix} -2 \\ 1 \\ -3 \end{bmatrix} = 0$$

$$l_2 : \left( r - \begin{bmatrix} -3 \\ 2 \\ 7 \end{bmatrix} \right) \times \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} = 0$$

$$l_3 : \left( r - \begin{bmatrix} -5 \\ 12 \\ -4 \end{bmatrix} \right) \times \begin{bmatrix} 4 \\ 0 \\ 9 \end{bmatrix} = 0$$









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- 13 Two light elastic strings each have one end attached to a particle  $B$  of mass  $3c$  kg, which rests on a smooth horizontal table.

The other ends of the strings are attached to the fixed points  $A$  and  $C$ , which are 8 metres apart.

$ABC$  is a horizontal line.



String  $AB$  has a natural length of 4 metres and a stiffness of  $5c$  newtons per metre.

String  $BC$  has a natural length of 1 metre and a stiffness of  $c$  newtons per metre.

The particle is pulled a distance of  $\frac{1}{3}$  metre from its equilibrium position towards  $A$ , and released from rest.

- 13 (a) Show that the particle moves with simple harmonic motion. [8 marks]

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14 (a) Given that

$$\sinh(A + B) = \sinh A \cosh B + \cosh A \sinh B$$

express  $\sinh(m + 1)x$  and  $\sinh(m - 1)x$  in terms of  $\sinh mx$ ,  $\cosh mx$ ,  $\sinh x$  and  $\cosh x$   
[1 mark]

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For Examiner's Use	
Question	Mark
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<b>TOTAL</b>	

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**GB/VW/Jun20/7367/1/E2**

