AQA

## Surname

Other Names
Centre Number
Candidate Number
Candidate Signature
I declare this is my own work.
GCSE
MATHEMATICS
Higher Tier Paper 3 Calculator 8300/3H

Time allowed: 1 hour 30 minutes
At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]


For this paper you must have:

- a calculator
- mathematical instruments.


## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is $\mathbf{8 0}$.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## ADVICE

In all calculations, show clearly how you work out your answer.

## DO NOT TURN OVER UNTIL TOLD TO DO SO

## Answer ALL questions in the spaces provided.

$1 b$ is 3 more than the square root of $a$.
Circle the correct equation. [1 mark]

$$
b=\sqrt{a}+3
$$

$$
b=\sqrt{a}-3
$$

$b=\sqrt{a+3}$
$b=\sqrt{a-3}$

2 Circle the largest number. [1 mark]
$0 . \dot{5}$
0.55
0.545
$0.5 \stackrel{\bullet}{5}$


## 5

3 A line has equation $3 y=3 x-2$
Circle the coordinates of the intercept
of the line with the $y$-axis. [1 mark]
$(0,1)$
$(0,-1)$
$\left(0, \frac{2}{3}\right) \quad\left(0,-\frac{2}{3}\right)$
4 Factorise $x^{2}-64$
Circle your answer. [1 mark]

$$
\begin{array}{ll}
(x+8)^{2} & (x-8)^{2} \\
(x+8)(x-8) & x(x-64)
\end{array}
$$

[Turn over]

5 Six positive numbers have a mean of 10
a range of 19
Four of the numbers are $\begin{array}{llll}12 & 7 & 15 & 3\end{array}$

Work out the other two numbers. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer <br> and

## [Turn over]



6 At a country park there is a house, a museum and a garden.

The table shows the prices per person to visit the park.

|  | Price per <br> person |
| :--- | :--- |
| Garden only | Free |
| House and museum | $£ 12.50$ |
| House only | $£ 8$ |
| Museum only | $£ 7$ |

One day, 480 people visit the park.
67 visit the garden ONLY.
$40 \%$ visit the house AND the museum.
$\frac{3}{8}$ visit the house ONLY.
The rest visit the museum ONLY.

9

## In total, how much do the 480 people pay to visit the park?

You may use the Venn diagram to help you. [5 marks]

$\qquad$
$\qquad$
[Turn over]


10

## Answer £

## 7 Jeff and Kaz share $£ 270$ in the ratio Jeff : Kaz = $2.6: 1$

How much MORE than Kaz does Jeff get? [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £
[Turn over]

8 The heel of a shoe exerts a pressure of 198 pounds per square inch.

Convert this pressure into kilograms per square centimetre.

Use
1 pound = 0.45 kilograms
1 square inch = 6.25 square centimetres [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer $\mathrm{kg} / \mathrm{cm}^{2}$

## [Turn over]

# 9 Rectangle $A B C D$ is split into four smaller rectangles. 

Two of the smaller rectangles are shaded.

The diagram is not drawn accurately.


4: $x=1: 2$

For rectangle $A B C D$, work out the ratio shaded area : unshaded area

## Give your answer in its simplest form. [4 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
:

## 10 A solid shape is drawn on isometric paper.

The gaps between the dots represent 1 centimetre.


## 10(a) On the grid below, draw the elevation of the shape from $A$.

The side of each square on the grid represents 1 centimetre. [1 mark]

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[Turn over]


REPEAT OF DIAGRAM


## 10(b) On the grid, draw a plan of the shape.

The side of each square on the grid represents 1 centimetre. [1 mark]

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[Turn over]

## 20

11 Erik thinks of a prime number between 20 and 30

His number is $\boldsymbol{x} \%$ of 125

Work out ONE possible value of $x$. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

21

## Answer

## [Turn over]



22
12 Part of a regular polygon with 15 sides is shown.

The diagram is not drawn accurately. '

Work out the size of an INTERIOR angle. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

23

## Answer <br> degrees

## [Turn over]

24

13 A box is the shape of half a cylinder on top of a cuboid.


Work out the volume of the box. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

25

Answer $\mathrm{cm}^{3}$

## [Turn over]



## 26

14 Phil sells ties.
He increases the original price of each tie by $\mathbf{1 0 \%}$ to $£ 13.20$

A month later he announces a sale.

```
SALE 10\% OFF ALL TIES
```

Phil says,
"The ties will be back to their original price, because each change was by $10 \%$ "

Is he correct?
Tick a box.


Yes


No

27

## Show working to support your answer. [3 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## 28

## 15 A biased spinner can land on A, B or C.

The table shows the probabilities, in terms of $k$, of A, B and C.


Work out the probability of $B$.
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

29

## Answer

## [Turn over]


$16 P$ is the point $(2,14)$
$Q$ is the point $(6,8)$
$R$ is the point $(2,5)$
Use gradients to show that angle $P Q R$ is NOT a right angle. [3 marks]
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$\qquad$
$\qquad$

31

## [Turn over]

Circle the possible value of $m$. [1 mark]

$$
\begin{array}{llll}
-2 \frac{7}{8} & 2.8 & 3 & -\frac{7}{2}
\end{array}
$$

18 Simplify $w^{\mathbf{1}} \times w^{\mathbf{0}}$
Circle your answer. [1 mark]
$10 \quad w \quad w^{2}$

19 The equation of a circle is $x^{2}+y^{2}=11$

Work out the length of the DIAMETER.
Circle your answer. [1 mark]
$\sqrt{11}$
$2 \sqrt{11}$
$\sqrt{22}$
22
[Turn over]

$20 \frac{a}{b}=3 c$
$\frac{b}{c}=2$
Work out the value of $a$ when $c=8$ [3 marks]

## Answer

35

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[Turn over]

36

21 Here is some information about the ages of babies at a clinic.

| Age, $x$ <br> (weeks) | Frequency |  |  |
| :--- | :--- | :--- | :--- |
| $0 \leqslant x<5$ | 18 |  |  |
| $5 \leqslant x<10$ | 23 |  |  |
| $10 \leqslant x<20$ | 17 |  |  |
| $20 \leqslant x<50$ | 21 |  |  |

On the opposite page, draw a histogram to represent the information. [4 marks]

37

[Turn over]
$\overline{7}$

22 A sequence of patterns is made using horizontal sticks and vertical sticks.


The table shows the number of horizontal sticks and vertical sticks in each pattern.

| Pattern | Number of <br> horizontal <br> sticks | Number of <br> vertical <br> sticks |
| :--- | :--- | :--- |
| 1 | 2 | 2 |
| 2 | 4 | 3 |
| 3 | 6 | 4 |

What fraction of the total number of sticks in Pattern $\boldsymbol{n}$ are horizontal?

Give your answer in terms of $\boldsymbol{n}$. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## [Turn over]



## 40

23 The equation of a curve is $y=16^{x}$
23(a) Circle the point that lies on the curve. [1 mark]
$(2,32)$
$(32,2)$
$(2,256)$
$(256,2)$

23(b) A different point on the curve has $y$-coordinate $\frac{1}{16}$

Work out the $x$-coordinate. [1 mark]
$\qquad$

Answer


## 41

$24 a^{b}=3 \quad$ where $a$ is an integer and $b$ is a proper fraction.

Work out ONE possible pair of values
of $a$ and $b$. [1 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$a=\square b=$
[Turn over]
6

## 42

25 Expand and simplify fully $(x-3)(x+2)(x+5) \quad$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$\qquad$

43

Answer

## [Turn over]

26 Here are two similar cones.

## Cone A Cone B



The surface area of cone $A$ is $\mathbf{2} \mathbf{m}^{\mathbf{2}}$

The surface area of cone $B$ is $4.5 \mathrm{~m}^{2}$

Work out the ratio radius of cone $A$ : radius of cone $B$

Give your answer in the form $1: n$ [3 marks]
$\qquad$
$\qquad$


45

Answer
:

## [Turn over]

27 In the diagram
$\overrightarrow{D E}=\mathrm{a}$
$\overrightarrow{D H}=\mathrm{b}$
$\overrightarrow{H G}=8 b$
$E X: X H=3: 1$
$E F: F G=1: 3$
The diagram is not drawn accurately.


## 47

27(a) Show that $\overrightarrow{D X}=\frac{1}{4} a+\frac{3}{4} b$

## [2 marks]

[Turn over]

48
BLANK PAGE

49

27(b) Is DXF a straight line?
Show working to support your answer. [4 marks]
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$\qquad$
[Turn over]

$28 a=4.72$ to 3 significant figures.
$b=158$ to 3 significant figures.
Work out the upper bound of $\frac{a}{b}$
You MUST show your working.
[3 marks]
$\qquad$
$\qquad$
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$\qquad$

Answer


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## [Turn over]

52
$29 A, B$ and $C$ are three points on the circumference of a circle, centre 0 .
$B D$ and $C D$ are tangents to the circle.
$A B D C$ is a kite.
Angle $B D C$ is $x$
The diagram is not drawn to scale.


Prove that angle $A B O$ is $45^{\circ}-\frac{x}{4}$
[4 marks]
$\qquad$
$\qquad$

53
[Turn over]

54
30 A sphere has radius $r$ cm

An approximate value of $r$ can be found using the iterative formula

$$
r_{n+1}=\sqrt{\frac{239}{r_{n}}}
$$

The starting value is $r_{1}=7$

30(a) Work out the values of $r_{2}$ and $r_{3}$ [2 marks]
$r_{2}=$
$r_{3}=$ $\qquad$

55

## 30(b) Continue the iteration to work out the radius to 1 decimal place. [1 mark]

## Answer

cm

## END OF QUESTIONS

$\overline{3}$

56

|  | Additional page, if required. <br> Write the question numbers in the <br> left-hand margin. |
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## 57

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## 58

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| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
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## IB/M/SB/Jun21/8300/3H/E2



