# A 

## AQAE

Surname $\qquad$
Other Names

Centre Number
Candidate Number
Candidate Signature
I declare this is my own work.

## GCSE <br> MATHEMATICS



Higher Tier
Paper 3 Calculator

## 8300/3H

Time allowed: 1 hour 30 minutes
At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## ADVICE

In all calculations, show clearly how you work out your answer.

DO NOT TURN OVER UNTIL TOLD TO DO SO

Answer ALL questions in the spaces provided.

1 Circle the smallest number. [1 mark]
4.31
$4.3^{\circ}$
4.301
4.33

2 Work out $\binom{-4}{8}-\binom{3}{-2}$
Circle your answer. [1 mark]

$$
\binom{-7}{10} \quad\binom{-7}{6} \quad\binom{-1}{10} \quad\binom{-1}{6}
$$

3 Here are four scatter graphs, on the opposite page.

## Graph A



Graph C


Graph B


Graph D


3(a) For which graph is a straight line of best fit appropriate?

Circle your answer. [1 mark]
A
B
C
D

3 (b) Which graph has ONE outlier?
Circle your answer. [1 mark]
A
B
C
D
[Turn over]


4 Use trigonometry to work out the size of angle $x$. The diagram is not drawn accurately.

[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

5 Laura works in a shop.
The table shows the number of hours she works on two weekends.

|  | Saturday | Sunday |
| :--- | :--- | :--- |
| Weekend 1 | 3 | 2 |
| Weekend 2 | $5 \frac{1}{2}$ | $3 \frac{1}{2}$ |

Work out the percentage increase in her TOTAL hours from Weekend 1 to Weekend 2 [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
\%

6 Here is a sketch of the curve $y=x^{2}-4 x-5$


6 (a) Write down the TWO roots of $x^{2}-4 x-5=0$ [1 mark]

6 (b) Work out the coordinates of $T$, the turning point of the curve. [2 marks]

## Answer ( <br> $\qquad$ ,

## [Turn over]

$7 \quad \mathrm{~A}$ is an ARITHMETIC progression.
Here are the first four terms.
$13 \quad 16 \quad 19 \quad 22$

G is a GEOMETRIC progression.
Here are the first four terms.
$\begin{array}{llll}2 & 4 & 8 & 16\end{array}$
$n$th term of $A=8$ th term of $G$

Work out the value of $\boldsymbol{n}$. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## $\boldsymbol{n}=$

[Turn over]


8 Information about two fridge-freezers, A and B, is shown.


TOTAL capacity is 330 litres
fridge capacity : freezer capacity $=3: 2$


FRIDGE capacity is 294 litres
fridge capacity : freezer capacity $=7: 3$

Grace buys one of these fridge-freezers.
She buys the one with the greater FREEZER capacity.

Which one does she buy?
You MUST show your working. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## Answer

$\boxed{4}$

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[Turn over]

9 Tom and Adil are the two runners in a 200-metre race.

Tom completes the race in $\mathbf{2 4}$ seconds.
Adil completes the race at an average speed of 28.8 kilometres per hour.

Who wins the race?
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]


10 The mass of a baby is 3.6 kilograms to 1 decimal place.

What is the error interval for the mass in kilograms?

Tick ONE box. [1 mark]


$$
3.5 \leqslant \text { mass } \leqslant 3.6
$$


$3.55 \leqslant$ mass $\leqslant 3.65$

$3.5 \leqslant$ mass < 3.6

$3.55 \leqslant$ mass < 3.65

11 A quadrilateral has angles $70^{\circ}, 110^{\circ}, 130^{\circ}$ and $50^{\circ}$

Circle the possible type of quadrilateral. [1 mark]
kite
rhombus
parallelogram
trapezium

## BLANK PAGE

[Turn over]


12(a) $B$ is
6 km due South of $A$
and
6 km due West of $C$.
The diagram is not drawn accurately.


Work out the bearing of $A$ from $C$. [2 marks]

Answer

12(b) Here is a scale drawing.


A ship is going to sail from $D$ to $E$.
Mia works out that the ship needs to sail on a bearing of $068^{\circ}$

Why must Mia be wrong? [1 mark]
[Turn over]


13 Simplify $\sqrt{5} a+\sqrt{5} a$
Circle your answer. [1 mark]
$\begin{array}{llll}5 a & 5 a^{2} & 2 \sqrt{5} a & \sqrt{10} a\end{array}$
4

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[Turn over]

14 Students in two classes, A and B, raised money for charity.

The box plot for class $\mathbf{A}$ is shown on the grid.


For class B,

- the lowest amount was $£ 3$ and the highest amount was $£ 26$
- the lower quartile was $£ 11$
- the median was $£ 2$ greater than the class $\mathbf{A}$ median
- the interquartile range was $1 \frac{1}{2}$ times greater than the class A interquartile range.

Draw the box plot for class B on the grid.
[4 marks]

## [Turn over]



15 A town has
a population density of 278 people per $\mathrm{km}^{2}$ and
a population of 158460
population density $=\frac{\text { population }}{\text { area }}$

The population increases to 168720
Work out the population density after the increase. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer people per $\mathbf{k m}^{\mathbf{2}}$
[Turn over]


16 Here is a scale drawing of a reservoir.
SCALE: 1 cm represents 500 m


Virat wants to estimate the volume of water in the reservoir.

He draws on the scale drawing a circle with radius 3 cm


16(a) Virat estimates the volume of the reservoir by assuming that

- the reservoir is a cylinder whose cross section is the circle
- the depth of the reservoir is $\mathbf{1 7}$ metres.

Work out Virat's estimate in cubic metres. [3 marks]
$\qquad$
$\qquad$
$\qquad$

Answer
$\mathrm{m}^{3}$
[Turn over]


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## 16 (b) In fact,

- the depth of the reservoir is 13.8 metres
- the reservoir is not a cylinder (see diagram).

Which statement about the actual volume of the reservoir is correct?

## Tick ONE box.



It is less than Virat's estimate


It is greater than Virat's estimate


Give a reason for your answer. [2 marks]
[Turn over]

17 In a video game, players make their own character.

They choose one of each from
8 faces
4 bodies
5 hairstyles.
17 (a) How many different characters can be made? [2 marks]

Answer $\qquad$

17 (b) Two characters are made at random.
What is the probability that they are exactly the same? [1 mark]

## Answer

[Turn over]
$18 \quad A, B$ and $C$ are points on a circle, centre $O$. $D C$ is a tangent to the circle.

The diagram is not drawn accurately


Show that angle $A B O$ : angle $A C O=3: 1$ [5 marks]
$\qquad$
$\qquad$
$\qquad$
[Turn over]

19 Here is the plan of the floor of an L-shaped room.

All lengths are in metres.
The diagram is not drawn accurately.


19(a) The area of the floor is $75 \mathrm{~m}^{2}$
Show that $x^{2}+x-90=0 \quad$ [3 marks]
[Turn over]

19(b) By factorising $x^{2}+x-90$ work out the value of $x$.

You MUST show your working [2 marks]
$\qquad$
$\qquad$
$\qquad$
$x=$

20
$£ 2448$ is invested in an account at a rate of compound interest.

One year after the investment there is $£ 2496.96$ in the account.

How much is in the account four years after the investment? [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £

## [Turn over]

$\boxed{8}$

21 The diagram is not drawn accurately.


Use the sine rule to work out the size of angle $x$. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$22 \mathrm{f}(x)=3 x$ and $\mathrm{g}(x)=x^{2}$
Circle the expression for $\mathrm{fg}(x)$ [1 mark]
$3 x^{2}$
$9 x^{2}$
$3 x^{3}$
$9 x^{4}$
[Turn over]


23 Here are two simultaneous equations.

$$
\begin{aligned}
& y=x^{2}+7 x-c \\
& \text { and } \\
& y=3 x+d
\end{aligned}
$$

There is a solution when $x=5$
Work out the value of $\boldsymbol{c}+\boldsymbol{d} \quad$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## 43

Answer
[Turn over]

24 Here is a sketch of the graphs of $y=k^{x}$ and $y=x^{2}+c$
$k$ and $c$ are positive constants.


Work out the value of $r$. [4 marks]
$\qquad$
$\qquad$
$\qquad$


## $r=$

## [Turn over]

A company makes tubes of toothpaste.
The masses of 80 tubes are checked.
A histogram is drawn to represent the data.

## Frequency density



The company makes 28000 tubes each day.
Estimate how many tubes each day have a mass LESS THAN 122 grams. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
[Turn over]
$Q$ and $R$ are two numbers.
As a product of prime factors,
$Q=2^{3} \times 3 \times a^{3}$
$R=2^{4} \times 3^{2} \times a^{2}$
26(a) The highest common factor (HCF) of $Q$ and $R$ is 4056

Work out the value of $a$. [2 marks]
$a=$ $\qquad$


## 26(b) Work out the lowest common multiple (LCM) of $Q$ and R. [2 marks]

Answer
[Turn over]

# 27 Expand and simplify fully $(x-3)(x-4)(x+8)$ [3 marks] 

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Answer

END OF QUESTIONS
$\qquad$
$\qquad$

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| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-5$ |  |
| $6-7$ |  |
| $8-11$ |  |
| $12-14$ |  |
| $16-18$ |  |
| $20-22$ |  |
| $24-27$ |  |
| $28-31$ |  |
| $32-35$ |  |
| $36-39$ |  |
| $40-43$ |  |
| $44-47$ |  |
| $48-51$ |  |
| TOTAL |  |

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