Surname
Other Names
Centre Number
Candidate Number
Candidate Signature
I declare this is my own work.
Level 2 Certificate
FURTHER MATHEMATICS
Paper 2 Calculator
8365/2
Time allowed: 1 hour 45 minutes
At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]


For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).


## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.
- In all calculations, show clearly how you work out your answer.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more graph paper and tracing paper. These must be tagged securely to this answer book.
- The use of a calculator is expected but calculators with a facility for symbolic algebra must NOT be used.


## DO NOT TURN OVER UNTIL TOLD TO <br> DO SO

# Answer ALL questions in the spaces provided. 

1 Factorise fully $12 w+18 w^{2}$ [2 marks]

## Answer

## $2 M$ is the midpoint of $P Q$.

The diagram is not drawn accurately.


5

Work out the value of $a$. [2 marks]

## Answer

## [Turn over]

6
3(a) Work out $3\left(\begin{array}{ll}4 & 2 \\ 1 & 0\end{array}\right)\left(\begin{array}{cc}2 & 0 \\ -1 & 5\end{array}\right)$

## Give your answer as a single matrix. [3 marks]

$$
\text { 3(b) }\left(\begin{array}{cc}
7 & a^{2} \\
b & -5
\end{array}\right)\binom{2}{a}=\binom{78}{12}
$$

Work out the values of $a$ and $b$. [3 marks]

[Turn over]

## 8

4 Line A has equation $y+4 x=6$
Line $B$ is parallel to line $A$ and passes through the point $(2,1)$

The point ( $d, 2 d$ ) lies on line B.
Work out the value of $d$. [4 marks]

## Answer

## 9

5 Work out all the NEGATIVE integer values of $x$ for which $3 x^{2}<48$ [3 marks]

## Answer

## [Turn over]

6 Prove algebraically that when $\boldsymbol{n}$ is an integer
$\frac{(2 n+1)^{2}-(2 n-1)^{2}}{4}$ is always even.
[3 marks]
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$\qquad$

7 How many integers between 200000 and 400000 can be formed using only the digits
1
2
3
5
8
9
with no repetition of any digit? [2 marks]

## Answer

[Turn over]

8 A curve has equation $y=x^{3}-5 x^{2}$
At two points on the curve, the rate of change of $y$ with respect to $x$ is 4

8(a) Work out an equation, in terms of $x$, to represent this information.

Give your answer in the form $a x^{2}+b x+c=0 \quad$ where $a, b$ and $c$ are integers. [2 marks]

Answer

# 8(b) Hence, work out the two possible values of $\boldsymbol{x}$. 

Give your answers to 3 significant figures. [2 marks]

## Answer

[Turn over]

9 The first three terms of a linear sequence are
$30 \quad 30+4 k \quad 30+8 k$
where $k$ is a constant.

9(a) Work out an expression, in terms of $k$, for the 4th term.

Give your answer in its simplest
form. [1 mark]

Answer

## 9(b) The 100th term of the sequence is 525

Work out the value of $\boldsymbol{k}$. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]

10 There are four sketch graphs on pages 16-18.

Circle the letter of the sketch graph that represents $y=3 \times 2^{x} \quad$ [1 mark]

A


17

B


C


## [Turn over]



D


## BLANK PAGE

## [Turn over]

20
11 Here is a right-angled triangle.
The diagram is not drawn accurately.

$(a-3) \mathrm{cm}$

## 21

## You are given that $a>5$

Use trigonometry to work out the range of values of $x$. [2 marks]

## Answer

22
12 Work out the gradient of the curve $y=\frac{12 x^{3}-8 x+3}{4 x^{2}}$ at the point where $x=-1$

You MUST show your working. [5 marks]
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$\qquad$

23

## Answer

## [Turn over]



24
$13 \quad A(-2,5)$ and $B(4,13)$ are points on a circle.
$A B$ is a diameter.
Work out the equation of the circle.
Give your answer in the form $(x-a)^{2}+(y-b)^{2}=c \quad$ where $a, b$ and $c$ are integers. [3 marks]
$\qquad$
$\qquad$
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$\qquad$

25

## Answer

## [Turn over]



26
14 PQRS is a cyclic quadrilateral.
The diagram is not drawn accurately.


## 27

Angle $P S R=4\left(x+15^{\circ}\right)$
Angle $P Q R$ is $40^{\circ}$ smaller than angle $P S R$.
Work out the value of $x$. [3 marks]
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$\qquad$
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$\qquad$

Answer
degrees
[Turn over]


## 28

15 Simplify fully $\left(\frac{x}{2}+\frac{3 x}{5}\right) \div \sqrt{\frac{x^{6}}{4}}$ [5 marks]

29

## Answer

[Turn over]

16 Here is an isosceles triangle.
All the angles are acute.
The diagram is not drawn accurately.


The area of the triangle is $120 \mathrm{~cm}^{2}$
Work out the size of angle $y$. [4 marks]

31

## Answer <br> degrees

## [Turn over]

17 Solve the simultaneous equations
$a+3 b-2 c=4$
$4 a-3 b+5 c=-5$
$2 a+b+3 c=9$
Do NOT use trial and improvement.
You MUST show your working.
[5 marks]
$\qquad$
$\qquad$
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$\qquad$
$\qquad$
$\qquad$
$33$


至 18 ABCDEFGH is a cuboid, on the opposite page.
$A B=40 \mathrm{~cm} \quad B C=9 \mathrm{~cm} \quad C G=20 \mathrm{~cm}$
$P$ is a point on $H G$ such that $H P: P G=3: 7$
$A P=25 \mathrm{~cm}$


બ
[Turn over]

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$\omega$

## Work out the size of angle APC. [5 marks]

$\qquad$ $\boldsymbol{\omega}$
[Turn over]

Answer

19 Expand and simplify fully $(3 x+4)(2 x-3)(5 x-2)$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $\xrightarrow{4}$

## Answer

[Turn over]

40

20 $f(x)=2 x^{3}+11 x^{2}+12 x-9$

20(a) Use the factor theorem to show that $(2 x-1)$ is a factor of $f(x)$. [2 marks]

20(b) Show that $f(x)=0$ has EXACTLY TWO solutions. [4 marks]
$\qquad$
$\qquad$

41
[Turn over]

## 42

21 Work out the values of $x$ between $0^{\circ}$ and $360^{\circ}$ for which
$2 \tan ^{2} x=3$
Give your answers to 1 decimal place.
You MUST show your working. [4 marks]
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43

## Answer

## [Turn over]

44

22 Using powers of 2 or otherwise, work out the non-zero value of $\boldsymbol{x}$ for which
$\left(16^{x}\right)^{x}=\frac{1}{2^{3 x}}$
You MUST show your working. [4 marks]
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45

## Answer

## END OF QUESTIONS

## 46

|  | Additional page, if required. <br> Write the question numbers in the <br> left-hand margin. |
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## 47

 | Additional page, if required. |
| :--- |
| Write the question numbers in the |
| left-hand margin. |

## 48

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| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-7$ |  |
| $8-11$ |  |
| $12-15$ |  |
| $16-21$ |  |
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| $44-45$ |  |
| TOTAL |  |

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