AQA

## Surname

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Centre Number
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I declare this is my own work.

## GCSE

MATHEMATICS


Higher Tier Paper 2 Calculator 8300/2H

Thursday 3 November 2022 Morning
Time allowed: 1 hour 30 minutes
At the top of the page, write your surname and forename(s), your centre number, your candidate number and add your signature.
[Turn over]


## MATERIALS

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).


## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

ADVICE
In all calculations, show clearly how you work out your answer.

DO NOT TURN OVER UNTIL TOLD TO
DO SO

Answer ALL questions in the spaces provided.

1 Work out $\frac{4^{6}-11}{\sqrt{625}-225}$

Circle your answer. [1 mark]

$$
-61.6 \quad-20.425
$$

204.25
3870.56

2 Work out $\left(3.1 \times 10^{9}\right)^{2}$

Circle your answer. [1 mark]

$$
\begin{array}{ll}
6.2 \times 10^{18} & 6.2 \times 10^{81} \\
9.61 \times 10^{18} & 9.61 \times 10^{81}
\end{array}
$$

## 5

3 The equation of a line is $y=3 x-6$
Circle the coordinates of the $y$-intercept. [1 mark]
$(0,-6)$
$(-6,0)$
$(0,3)$
$(3,0)$
$4 \quad a \times b^{4}=c$

Circle the correct expression for $a$. [1 mark]

$$
\frac{c}{\sqrt[4]{b}} \quad \frac{c}{b^{-4}} \quad\left(\frac{c}{b}\right)^{4} \quad \frac{c}{b^{4}}
$$

[Turn over]


6

5 Written as the product of prime factors,
$12600=2^{3} \times 3^{2} \times 5^{2} \times 7$ and

$$
14112=2^{5} \times 3^{2} \times 7^{2}
$$

Work out the highest common factor (HCF) of 12600 and 14112

Give your answer as an integer. [2 marks]
$\qquad$
$\qquad$
$\qquad$

## Answer

6

## BLANK PAGE

## [Turn over]

6 The composite bar chart, on the opposite page, shows information about the PERCENTAGE of drinks sold by a café in 2007 and 2019

6 (a) In 2007 the café sold a total of 24000 drinks.

How many MORE teas than
coffees were sold? [ 2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

9
KEY:
$\square$ Coffee $\square$ Tea $\square$ Other

Percentage of drinks sold

[Turn over]

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6 (b) Were more coffees sold at the café in 2019 than in 2007 ?

Tick a box.


Yes

$\square$ Cannot tell
Give a reason for your answer. [1 mark]
[Turn over]


# 7 (a) $k$ is a whole number between 40 and 50 

The cube root of $k$ is 3 , to the nearest whole number.

Work out the LARGEST possible value of $k$. [2 marks]

## Answer

7 (b) Fay tries to solve $x^{2}=100$
She says, "The only possible value of $x$ is 10 "

Give a reason why she is NOT correct. [1 mark]
[Turn over]
6

## 8 (a) Here is a cuboid.

$w, x$ and $y$ are DIFFERENT whole numbers.


The total length of ALL the edges of the cuboid is $\mathbf{8 0} \mathbf{~ c m}$

The volume is GREATER than $200 \mathrm{~cm}^{3}$

Work out one possible set of values for $w, x$ and $y$. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $w=$
$x=$
$y=$

## [Turn over]

## 8 (b) Here is a solid cube.


$3 a \mathrm{~cm}$

Circle the expression for the TOTAL surface area in $\mathrm{cm}^{2}$ [1 mark]
$36 a$
$54 a$
$36 a^{2}$
$54 a^{2}$

# 9 The 47th triangular number is 1128 

The 48th triangular number is 1176
Work out the 49th triangular number. [1 mark]
$\qquad$

Answer
[Turn over]
4


10 The $n$th terms of two linear sequences, $A$ and $B$, are added to give the $n$th term of a new sequence.

The new sequence starts
8
13
18
23

The $n$th term of sequence $A$ is n+1

Work out the $n$th term of sequence $B$. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## [Turn over]

20
11 A tank contains 40 litres of water.
11 (a) Water leaks out of the tank at a rate of 1.2 litres per minute.

The leak is stopped after 20 minutes.

Show that, when the leak is stopped, the tank contains 16 litres of water. [1 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

21

## BLANK PAGE

## [Turn over]

22
11 (b) The tank is refilled with water from a tap.

The graph shows the amount of water in the tank AFTER the leak is stopped.

Water in tank
(litres)


Time (minutes)

## 23

Complete this report by writing a number in each answer space. [3 marks]

REPORT
minutes after the
leak is stopped, the tap starts to refill the tank.

The rate at which the tank refills is
litres per minute.

## 24

12 The length of this rectangle is 6 times the width.

The diagram is not drawn accurately.

## $6 x$



Two of these rectangles are joined, with no overlap, to make the L-shape on page 25.

## 25

The diagram, on the opposite page, is not drawn accurately.

[Turn over]

26

BLANK PAGE

## 27

## The perimeter of the L-shape is 98.8 cm

Work out the value of the perimeter of ONE of the rectangles. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## 28

13 Trapezium DEFG is formed by joining triangle DEH to rectangle EFGH.

The diagram is not drawn accurately.


29

## $A B C$ is similar to $D E H$.

Work out the area of DEFG. [5 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
$\mathrm{cm}^{2}$

## [Turn over]



14 Fred bought an apartment for £137500

He made 8\% profit when he sold the apartment.

He used all of this profit to pay 40\% of the deposit on a house.

The deposit was one sixth of the price of the house.

Work out the price of the house. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

31

Answer £

## [Turn over]

15 Circle the correct statement. [1 mark]

$1 \mathrm{~m}^{2}=100 \mathrm{~mm}{ }^{2}$

## $1 \mathrm{~cm}^{2}=100 \mathrm{~mm}^{2}$

$1 \mathrm{~m}^{2}=100 \mathrm{~cm}^{2}$
1 km² $=100 \mathrm{~m}^{2}$

## BLANK PAGE

## [Turn over]

16 Here is a sketch of a graph.


## 35

Circle the possible equation of the graph. [1 mark]

$$
\begin{array}{ll}
y=x^{2}+1 & y=\frac{1}{x}+1 \\
y=x^{3}+1 & y=1-x^{2}
\end{array}
$$

17 A sequence of numbers is formed by the iterative process

$$
u_{n+1}=\frac{20}{u_{n}+3} \text { where } u_{1}=1
$$

Work out $\boldsymbol{u}_{3}$

Circle your answer. [1 mark]
$\begin{array}{llll}\frac{40}{11} & \frac{5}{2} & 7 & 5\end{array}$
[Turn over]

18 A basketball team plays 19 home games and 19 away games.

The box plot shows information about the points the team scored in HOME games.


Here are the points the team scored in the 19 AWAY games.

| 85 | 89 | 93 | 95 | 96 | 96 | 98 | 98 | 98 | 99 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 100 | 103 | 105 | 107 | 109 | 110 | 114 | 119 | 126 |  |

18(a) On the grid opposite, draw a box plot for the away games. [4 marks]
[Turn over]

18 (b) On average, did the team score more points in home games or away games?

Use ONE statistical measure to support your decision. [1 mark]

18 (c) Was the number of points scored more consistent in home games or away games?

Use ONE statistical measure to support your decision. [1 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## 40

19 Using the quadratic formula, or otherwise, solve $3 x^{2}+x-5=0$ [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## BLANK PAGE

## [Turn over]

20 A vending machine has a different item in each section.

It sells
7 drinks, 3 of which are juice
5 snacks, 2 of which are fruit bars
11 meals, 4 of which are salad.
One drink, one snack and one meal are chosen at random.

Show that the probability of getting a juice, a fruit bar and a salad is MORE than 5\% [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

43
[Turn over]

44
$21 \quad f(x)=\frac{3 x+9}{5}$ and $g(x)=6 x-1$

21 (a) Show that $g f(2)$ is an integer. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## 45

## 21(b) Show that $\mathrm{f}^{-1}(8)$ is NOT an integer. [2 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]


## 46

22 Factorise fully $x^{3}-49 x \quad$ [2 marks]

## Answer

## BLANK PAGE

## [Turn over]

2361 students recorded how many hours they spent revising for a test.

The histogram represents the results.

Frequency density


Time (hours)
23 (a) Work out an estimate of the mean time the 61 students spent revising.

49

## You may use the table to help you. [4 marks]

| Time, $x$ <br> (hours) | Frequency | Midpoint |  |
| :---: | :--- | :--- | :--- |
| $0 \leqslant x<6$ |  |  |  |
| $6 \leqslant x<10$ |  |  |  |
| $10 \leqslant x<12$ |  |  |  |
| $12 \leqslant x<16$ |  |  |  |
| $16 \leqslant x<20$ |  |  |  |

$\qquad$
$\qquad$
$\qquad$

Answer
hours
$||||||||||||||\mid$ [Turn over]

50

BLANK PAGE

51

## 23 (b) Give a reason why the answer to part (a), on pages 48 to 49, is an estimate. [1 mark]

[Turn over]
7
$24 B$ is 60 miles from $A$ on a bearing of $170^{\circ}$

The diagram is not drawn accurately.


A ship sails from A on a bearing of $247^{\circ}$

It travels at a constant speed of 23 mph for $1 \frac{1}{2}$ hours.

Is the ship now closer to $B$ than it was when it left $A$ ?

You MUST show your working. [5 marks]

## [Turn over]



54

55

## BLANK PAGE

## [Turn over]

56
25 Two congruent parallelograms, PQRV and VRST, are joined.

The diagram is not drawn accurately.

$X$ is the midpoint of $V T$.
$V W: W R=1: 2$
Prove that $Q, W$ and $X$ lie on a straight line. [3 marks]
$\qquad$


57
[Turn over]

26 Helena ran an 800-metre race in 140 seconds.

The speed-time graph represents the first 100 seconds of her run.

Speed
(m/s)

Helena ran the last 40 seconds with constant deceleration.
Work out her speed as she finished the race. [4 marks]

59

Answer
metres per second
[Turn over]


27 In a class there are
$n$ boys
a total of 25 students.

Two of the students are chosen at random.

The probability that both students are boys is $\frac{7}{20}$

Work out the value of $\boldsymbol{n}$. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

61

## $\boldsymbol{n}=$

[Turn over]


62

## $28 \quad A B C D E F$ is a triangular prism.

$P$ is a point on $E F$.

$E B=29 \mathrm{~cm}$
Angle EBP $=35^{\circ}$
Angle $E P B=114^{\circ}$
Work out the length of $E P$.
[2 marks]


## 63

## Answer



END OF QUESTIONS

## 64

$\qquad$

65

|  | Additional page, if required. <br> Write the question numbers in the <br> left-hand margin. |
| :--- | :--- |
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## 66

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| For Examiner's <br> Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-6$ |  |
| $8-13$ |  |
| $14-17$ |  |
| $18-23$ |  |
| $24-29$ |  |
| $30-35$ |  |
| $36-40$ |  |
| $42-45$ |  |
| $46-51$ |  |
| $52-57$ |  |
| $58-61$ |  |
| $62-63$ |  |
| TOTAL |  |

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