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I declare this is my own work.

A-level

FURTHER MATHEMATICS

Paper 3 Statistics

7367/3S

Wednesday 14 June 2023 Afternoon

Time allowed: 2 hours

At the top of the page, write your surname and forename(s), your centre number, your candidate number and add your signature.

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MATERIALS

For this paper you must have:

- **the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics**
- **a graphical or scientific calculator that meets the requirements of the specification**
- **the other optional Question Paper/Answer Book for which you are entered (EITHER Discrete OR Mechanics). You will have 2 hours to complete BOTH papers.**

INSTRUCTIONS

- **Use black ink or black ball-point pen. Pencil should only be used for drawing.**
- **Answer ALL questions.**
- **You must answer each question in the space provided for that question. Do NOT write outside the box around each page or on blank pages.**
- **If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).**
- **Show all necessary working; otherwise marks for method may be lost.**
- **Do all rough work in this book. Cross through any work that you do not want to be marked.**



INFORMATION

- **The marks for questions are shown in brackets.**
- **The maximum mark for this paper is 50.**

ADVICE

- **Unless stated otherwise, you may quote formulae, without proof, from the booklet.**
- **You do not necessarily need to use all the space provided.**

DO NOT TURN OVER UNTIL TOLD TO DO SO



Answer ALL questions in the spaces provided.

- 1 The discrete random variable A takes only the values 0, 2 and 4, and has cumulative distribution function $F(a) = P(A \leq a)$

a	0	2	4
$F(a)$	0.2	0.6	1

Find $P(A = 2)$

Circle your answer. [1 mark]

0

0.4

0.6

0.8



- 2 The time, T days, between rain showers in a city in autumn can be modelled by an exponential distribution with mean 1.25

Find the distribution of the number of rain showers per day in the city.

Tick (✓) ONE box. [1 mark]

	DISTRIBUTION	MEAN
<input type="checkbox"/>	Exponential	0.8
<input type="checkbox"/>	Exponential	1.25
<input type="checkbox"/>	Poisson	0.8
<input type="checkbox"/>	Poisson	1.25

[Turn over]



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- 4 The random variable X has a normal distribution with unknown mean μ and unknown variance σ^2

A random sample of 8 observations of X has mean $\bar{x} = 101.5$ and gives the unbiased estimate of the variance as $s^2 = 4.8$

The random sample is used to conduct a hypothesis test at the 10% level of significance with the hypotheses

$$H_0 : \mu = 100$$

$$H_1 : \mu \neq 100$$

Carry out the hypothesis test. [5 marks]



5 A school management team oversees 11 different schools.

The school management team allows each student in the schools to choose one enrichment activity from 11 possible activities.

The school management team count the number of students in each school choosing each of the possible activities. They then conduct a χ^2 -test for association with the data they have gathered.

5(a) Exactly one of the calculated expected frequencies for the χ^2 -test is less than 5

Explain why the number of degrees of freedom for the test is 90 [2 marks]



- 5(c) During the hypothesis test, the value of $\frac{(O - E)^2}{E}$, where O is the observed frequency and E is the expected frequency, was calculated for each group of students.

The values for four groups of students are shown in the table below.

GROUP	$\frac{(O - E)^2}{E}$
Attends school 3 and chose activity 1	0.01
Attends school 8 and chose activity 3	18.5
Attends school 8 and chose activity 7	24.2
Attends school 11 and chose activity 7	49.0

State, with a reason, which of the four groups of students represents the strongest source of association. [1 mark]

[Turn over]



6 A game consists of two rounds.

The first round of the game uses a random number generator to output the score X , a real number between 0 and 10

6(a) Find $P(X > 4)$ [1 mark]



7 Company A uses a machine to produce toys.

The number of toys in a week that do not pass Company A's quality checks is modelled by a Poisson distribution X with standard deviation 5

The machine producing the toys breaks down.

After it is repaired, 16 toys in the next week do not pass the quality checks.

7(a) Investigate whether the average number of toys that do not pass the quality checks in a week has changed, using the 5% level of significance. [7 marks]

[Turn over]



7 (b) For the test carried out in part (a), state in context the meaning of a Type II error. [1 mark]

[Turn over]



7(c) Company B uses a different machine to produce toys.

The number of toys in a week that do not pass Company B 's quality checks is modelled by a Poisson distribution Y with mean 18

The variables X and Y are independent.

Find the distribution of the total number of toys in a week produced by companies A and B that do not pass their quality checks.
[1 mark]



7(d) State TWO reasons why a Poisson distribution may not be a valid model for the number of toys that do not pass the quality checks in a week. [2 marks]

Reason 1 _____

Reason 2 _____

[Turn over]



- 8 The continuous random variable X has probability density function

$$f(x) = \begin{cases} k \sin 2x & 0 \leq x \leq \frac{\pi}{6} \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

- 8(a) Show that $k = 4$ [4 marks]



**8 (b) Find the cumulative distribution function $F(x)$
[3 marks]**

[Turn over]



8(c) Find the median of X , giving your answer to three significant figures. [2 marks]

8(d) Find the mean of X giving your answer in the form $\frac{1}{a}(b\sqrt{3} - \pi)$ where a and b are integers.

[5 marks]

[Turn over]



END OF QUESTIONS



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Additional page, if required.

Write the question numbers in the left-hand margin.

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For Examiner's Use	
Question	Mark
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