## AQA

Please write clearly in block capitals.

Centre number


Candidate number


Surname $\qquad$
Forename(s)
Candidate signature
I declare this is my own work.

## GCSE

MATHEMATICS

## Higher Tier Paper 1 Non-Calculator

Friday 19 May 2023
Morning
Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- mathematical instruments
- the Formulae Sheet (enclosed).

You must not use a calculator.


## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $2-3$ |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| TOTAL |  |

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## Advice

In all calculations, show clearly how you work out your answer.

1 (a) Work out $0.7 \times 0.5$

## Answer

1 (b) Work out $\frac{5}{6} \div 3$
$\qquad$
$\qquad$

Answer

1 (c) Work out $27 \div 0.6$
[1 mark]

Answer

| 2 | Solve $2 x<26$ | [1 mark] |
| :--- | :--- | :--- | :--- |
| Answer |  |  |
| Work out the value of $\left(\frac{3}{2}\right)^{2}$ |  |  |
| Give your answer as a mixed number. | [1 mark] |  |

## Answer

3 Work out the value of $\left(\frac{3}{2}\right)^{2}$
Give your answer as a mixed number.

## Answer

$\qquad$

## Turn over for the next question

$4 \quad A B C, B D$ and $B E$ are straight lines.


Not drawn accurately
angle $E B D=5 \times$ angle $A B E$
angle $D B C=3 \times$ angle $A B E$
Work out the size of angle EBD.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer -

5 Two prime numbers are multiplied together.
The answer is an even number between 50 and 60
Complete the calculation.


6 Andrew and Bruce share some money in the ratio 5:6
Bruce gets $£ 96$
Andrew gives $\frac{1}{4}$ of his share to Carl.
Bruce gives $\frac{2}{3}$ of his share to Carl.
How much money does Carl receive?
[4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £ $\qquad$
$7 \quad 2^{a} \times 3 \times 5^{2}=600$
Work out the value of $a$.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
a=
$$

$\qquad$

8 Expand and simplify fully $5(3 x+4)-2(x-1)$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
$9 \quad$ Erika tries to sketch the graph $\quad y=\frac{1}{x} \quad$ with $x \neq 0$


Make two different criticisms of her sketch.

Criticism 1
$\qquad$
$\qquad$
Criticism 2 $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

10 Sunita is $x$ years old.
Beth is one year younger than Sunita.
Joel is double Sunita's age.
The mean of their ages is 5
How old is Joel?
$\qquad$
$\qquad$
$\qquad$
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$\qquad$

Answer

11 The Venn diagram represents 100 items.


11 (a) Write down $P(A \cap B)$

Answer

11 (b) Work out $P\left(A^{\prime}\right)$
$\qquad$
$\qquad$

Answer

11 (c) Work out $P(A \cup B)$
$\qquad$
$\qquad$

Answer $\qquad$

12 (a) $a \times 10^{n}$ is a number in standard form.
Complete the inequality for the value of $a$.

$$
\leqslant a<
$$

$\qquad$

12 (b) $\quad b \times 10^{n}$ is the number 7200 written in standard form.
Work out $b \times 10^{-n}$
Write your answer as an ordinary number.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

13 (a) Here is a number machine.


Show that when the input increases by 2 the output increases by $2 a$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

13 (b) $\mathrm{f}(x)=k x^{2} \quad$ where $k$ is a constant.
Kai says that $\frac{f(6)}{f(2)}$ is equal to $f(3)$ because $\frac{6}{2}=3$
Is he correct?
Show working to support your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

14 Here is a list of 11 whole numbers in numerical order.
The lower quartile, median, upper quartile and highest value are missing.

| 5 | 8 |  | 13 | 19 |  | 25 | 28 |  | 34 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

- median $=2 \times$ lower quartile
- upper quartile $=2.5 \times$ lower quartile
- range $=2 \times$ interquartile range

Complete the list.
[2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$15 \quad A B C D$ is a trapezium.
All four sides are different lengths.
$A B$ is parallel to $C D$.
The diagonals intersect at $X$.


Not drawn accurately

For each statement, tick the correct box.

Triangles $A X B$ and $C X D$ are similar

Triangles $A X D$ and $B X C$ are congruent


Angle $A D B=$ angle $B D C$

Area of triangle $A B C=$ area of triangle $A B D$


May be true
Not true


## Turn over for the next question

16 Solve the simultaneous equations

$$
\begin{aligned}
& 2 x-5 y=13 \\
& 3 x+4 y=8
\end{aligned}
$$

$\qquad$
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$\qquad$
$\qquad$ $x=\quad y=$ $\qquad$

17 A solid hemisphere has radius $x$.
A solid cylinder has radius $3 x$ and height $x$.


Surface area of a sphere $=4 \pi r^{2}$ where $r$ is the radius

Work out the ratio
total surface area of the hemisphere : total surface area of the cylinder Give your answer in its simplest form.
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ : $\qquad$

| $6<\sqrt[3]{x}<7$ |  |  |
| :---: | :---: | :---: |
| Circle the possible value of $x$. |  |  |
| [1 mark] |  |  |
| 1.9 | 20 | 45 |

19 Work out how many 5-digit odd numbers can be made using these digits once each.
2
4
6
7
9

Do not list them.
[2 marks]

Answer $\qquad$

## $20 \mathrm{~K}, \mathrm{~L}$ and M are weights.

Both of the scales balance exactly.


How many $M$ weights are needed to balance one $L$ weight?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

Turn over for the next question

21 Express $x^{2}-6 x-15$ in the form $(x-a)^{2}-b \quad$ where $a$ and $b$ are integers.

Answer $\qquad$
$a=\sqrt{2} \quad$ and $b=\sqrt{18}$
Match each expression to its value.
One has been done for you.


23 Write 0.13 as a fraction in its simplest form.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$\qquad$

Answer

## r

24 Points $P, Q$ and $R(8,22)$ form a triangle.


Not drawn accurately
$P Q$ is a horizontal line, with $P$ on the $y$-axis.
Angle $P R Q$ is a right angle.
The gradient of $P R$ is 2
Work out the coordinates of $Q$.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$

Answer ( $\qquad$ , $\qquad$ )

25 Show that $\frac{4 \sin 30^{\circ}-\tan 45^{\circ}}{2 \cos 30^{\circ}}$ can be written as $\tan x$, where $x$ is an acute angle. [4 marks]
$\qquad$
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Turn over for the next question

26 A circle, centre $O$, has circumference $20 \pi \mathrm{~cm}$
$Q$ is a point on the circle.
$O P Q R$ is a square.
Not drawn accurately

perimeter of the square : circumference of the circle $=\sqrt{a}: \pi \quad$ where $a$ is an integer.
Work out the value of $a$.
You must show your working.
$\qquad$
$\qquad$ $\longrightarrow$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$a=$

27 A journey has two stages.

|  | Distance <br> $\mathbf{( k m )}$ | Average <br> speed <br> $(\mathbf{k m} / \mathbf{h})$ | Time <br> $\mathbf{( h )}$ |
| :---: | :---: | :---: | :---: |
| Stage 1 | 30 | $a$ | $\frac{30}{a}$ |
| Stage 2 | 30 | $b$ | $\frac{30}{b}$ |

Show that the average speed for the whole journey, in $\mathrm{km} / \mathrm{h}$, is $\frac{2 a b}{a+b}$
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There are no questions printed on this page
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