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Candidate Number	
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I declare this is my own work.	

GCSE STATISTICS

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Higher Tier Paper 2

8382/2H

Monday 19 June 2023

Afternoon

Time allowed: 1 hour 45 minutes

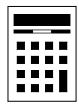
At the top of the page, write your surname and forename(s), your centre number, your candidate number and add your signature.



MATERIALS

For this paper you must have:

- a calculator
- mathematical instruments.



INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross out any work you do not want to be marked.



INFORMATION

- The marks for the questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper and graph paper. These must be tagged securely to this answer booklet.

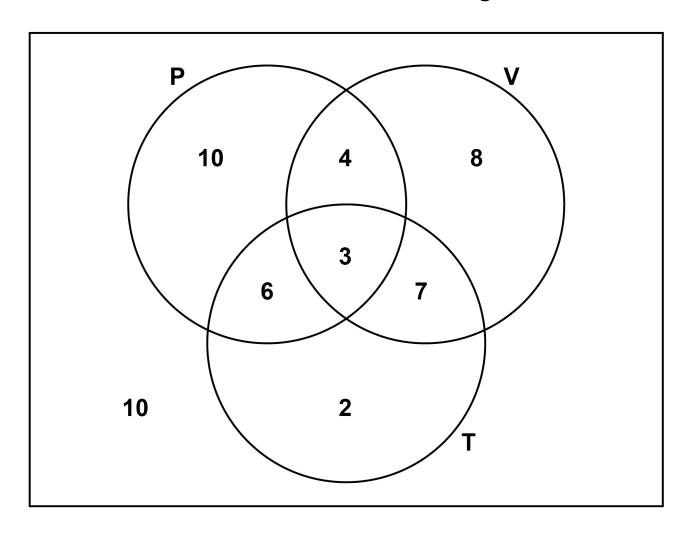
DO NOT TURN OVER UNTIL TOLD TO DO SO



Answer ALL questions in the spaces provided.

- 1 Tirunesh asks 50 people which of the following instruments they play,
 - piano (P)
 - violin (V)
 - trombone (T).

The results are shown in the diagram.





Tirunesh chooses one person at random.

1 (a) Circle the probability that this person plays the piano. [1 mark]

$$\frac{22}{50}$$

1 (b) Circle the value of P(V | T). [1 mark]

$$\frac{7}{18}$$

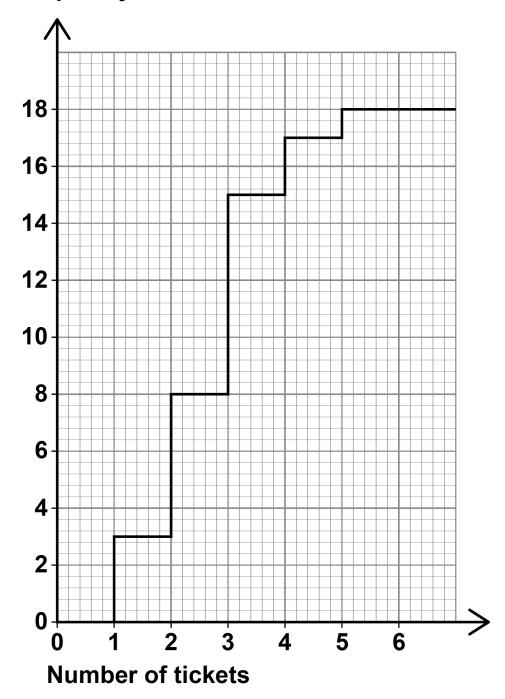
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2



The cumulative frequency step polygon represents the number of tickets bought by 18 customers one morning.

Cumulative frequency





Circle the number of customers who bought 3 tickets. [1 mark]

5 7 8 15

[Turn over]

1



Tony is investigating students' scores in statistics exams.

He says that it depends on the following factors,

- time spent studying
- score in maths exams.

Circle the term that best describes the type of data Tony uses. [1 mark]

bivariate multivariate

qualitative categorical

1



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The table shows information about births in the UK in 2010 and 2019.

	YEAR	
	2010	2019
NUMBER OF BIRTHS	807 300	712 700
TOTAL POPULATION	62 260 000	66 650 000
BIRTH RATE		10.7

Source: ONS

4 (a) Complete the table by finding the birth rate in 2010.

Use the formula

birth rate =
$$\frac{\text{number of births}}{\text{total population}} \times 1000$$

[2 marks]



4 (b)	The birth rate in Iceland in 2019 was 12.5
	Jack concludes,
	"Iceland had a higher number of births than the UK in 2019 because it had a higher birth rate."
	Comment on Jack's conclusion. [1 mark]
[Turn o	ver] 3



5	An app allows students to complete work set by their teacher.
	Mr Roper wants to test the effectiveness of the app in an experiment.
	He tells his class of 30 students that they have a test next week.
	To revise, he gives the app to half of the class, whilst the other half just use their books.
	Mr Roper ensures that there are the same numbers of boys and girls in each group.
5 (a)	Name ONE other consideration for Mr Roper when grouping the students. [1 mark]
5 (b)	The test scores for the APP GROUP are shown in the stem-and-leaf diagram, on the opposite page



4	5			
5	2	3	7	
6	4	5	6	8
7	0	3	5	7
8	1	9		
9	2			

KEY: 4 | 5 represents 45%

5 (b) (i)	Work out the median score. [1 mark]	
	Answer	_ %
5 (b)(ii)	Show that the interquartile range is 20% [2 marks]	



5 (c) The percentage scores of the 15 students who were in the BOOK GROUP are,

71	46	57	37	50
44	69	40	58	83
42	56	39	55	79

Use these results to complete the back-to-back stem-and-leaf diagram, on the opposite page, that shows both sets of results on the same diagram.

Remember to complete the key and the labels for the diagram. [4 marks]



				APF	GR	OUP	
			4	5			
			5	2	3	7	
			6	4	5	6	8
			7	0	3	5	7
			8	1	9		
			9	2			

KEY represent

5 (d) Using your stem-and-leaf diagram and the values from PART (b),

compare statistically the scores in the test for those who revised using the app and those who used their books. [5 marks]

[T.....



-		
-		
-		
-		



5 (e)	Give ONE criticism of the experime Mr Roper. [1 mark]	ent set up by
Turn (over]	14



Frieda, Piran and Elliot are investigating the most popular type of ice cream or ice lolly of the 1200 students at their school.

They want to take a sample of 60 students.

They each suggest a sampling method to collect the data.

FRIEDA'S METHOD

Ask the first 60 students who arrive at school.

PIRAN'S METHOD

Number each student on the register from 1 to 1200

Use a random number generator to find a starting point between 1 and 20

Choose to ask every 20th student after the starting point.

ELLIOT'S METHOD

For each year group, put all the names of the students in a hat.

Pick 5% of the names out for each year group.

Ask each of these students.



6 (a)	Write down the name of Frieda's method. [1 mark] Answer
6 (b) (i)	Write down ONE advantage of Piran's method. [1 mark]
6 (b)(ii)	Write down ONE disadvantage of Piran's method. [1 mark]



6 (c) (i)		wn the name of the sampling ie Elliot suggests. [1 mark]	J
6 (c) (ii)		e shows the number of stude ar group at their school.	ents in
	YEAR	NUMBER OF STUDENTS	
	7	260	
	8	200	
	9	178	
	10	280	
	11	282	
		e the number of students Elli from YEAR 7 [2 marks]	ot should

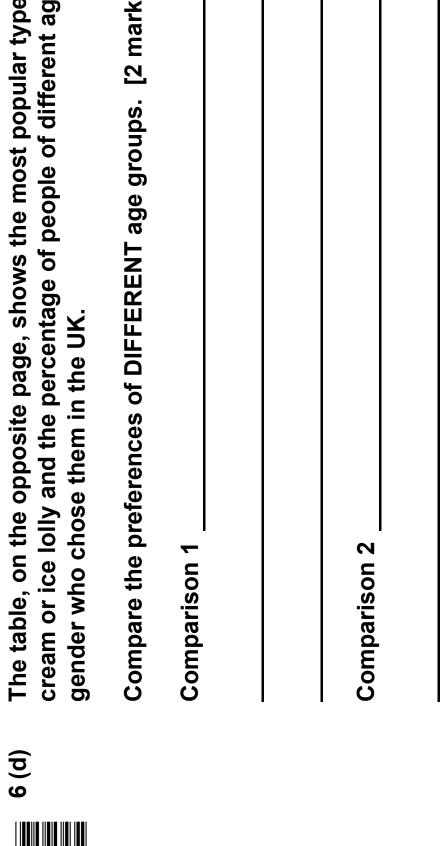


Answer

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	(p) 9	The table, on the opposite page, shows the most popular types of ice cream or ice lolly and the percentage of people of different ages and gender who chose them in the UK. Compare the preferences of DIFFERENT age groups. [2 marks] Comparison 1 Comparison 1
--	-------	---





		GENDER (%)	:R (%)	AGE C	AGE CATEGORY (%)	(%) X	
ICE CREAM OR ICE LOLLY	AII	Male	Female	18–24	25–49	50–64	65 +
Magnum	28	27	28	12	22	68	42
Fab	8	6	8	11	11	9	1
Solero	8	9	6	2	8	8	2
Twister	7	9	2	11	10	2	2
Feast	9	9	2	9	6	9	1
Calippo	5	9	4	2	9	3	2
Orange	3	3	2	1	1	3	10
Cornetto	3	2	3	2	3	2	1
Other	32	36	32	43	30	31	34

Source: adapted from YouGov



7	Leanne wants to buy a ticket to fly from
	Manchester to Greece next year.

Tickets are released by the airline exactly SIX months in advance of departure.

She investigates how the price of tickets changes over these six months.

She draws a scatter graph, on the opposite page, showing the ticket price, $\pounds P$, plotted against the time in months, t, since the tickets were released.

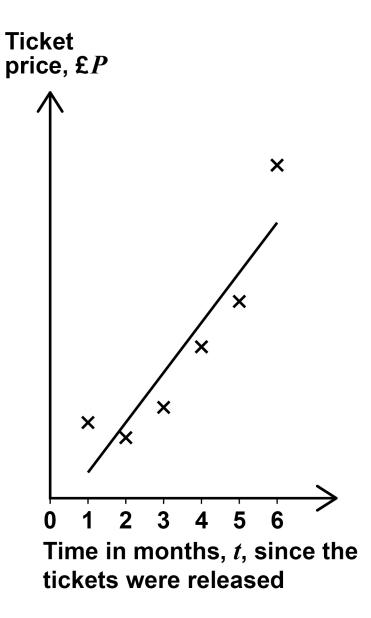
Leanne calculates that the equation of the regression line for her data is,

$$P = 32t - 16$$

7 (a) Interpret the value of 32 in Leanne's equation.

Give your answer in context. [1 mark]







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7 (b)	Leanne does not want to pay more than £100 for her ticket next year.
	Use the equation of the regression line to predict the latest time after tickets are released that Leanne could buy a ticket. [2 marks]
	Answer months
7 (c)	Give a reason, in context, why the regression equation is NOT appropriate when the tickets are initially released. [1 mark]



7 (d)	The product moment correlation coefficient for Leanne's data is 0.91
	Leanne says,
	"This shows there is a strong linear relationship."
	Looking at the scatter graph, is Leanne's conclusion appropriate?
	Tick (✓) a box.
	Yes
	No
	Give a reason for your answer. [1 mark]
	5



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The table shows average house prices in the UK.

YEAR	AVERAGE PRICE (£)
2016	283 000
2017	280 000

Source: ONS

8 (a)	Comment on the reliability of the source of the
	data. [1 mark]

8 (b)	Using 2016 as the base year, show that the
	index number for 2017, to 1 decimal place, is
	98.9 [1 mark]



8 (c)	Using 2016 as the base year, the index number for 2020 is 107.0
8 (c) (i)	A house purchased in 2016 cost £430 000
	Calculate an estimate for the value of this house in 2020. [2 marks]
	Answer £



8 (c) (ii)	Carla bought a house for £215 000 in 2016 and sold it for £233 000 in 2020.
	Did Carla's house increase by a GREATER proportion than the index number for 2020 suggests?
	Tick (✓) a box.
	Yes
	No
	You MUST show your working. [2 marks]
8 (d)	The table, on the opposite page, shows some index numbers relating to average house prices for a town.



YEAR	INDEX NUMBER
2017	100
2019	96.2
2021	104.2

2021	104.2
Andy say	ys,
•	e house prices in the town increased om 2019 to 2021."
Is Andy'	s conclusion valid?
Tick (√)	a box.
Y	es
N-	0
Give a re	eason for your answer. [1 mark]

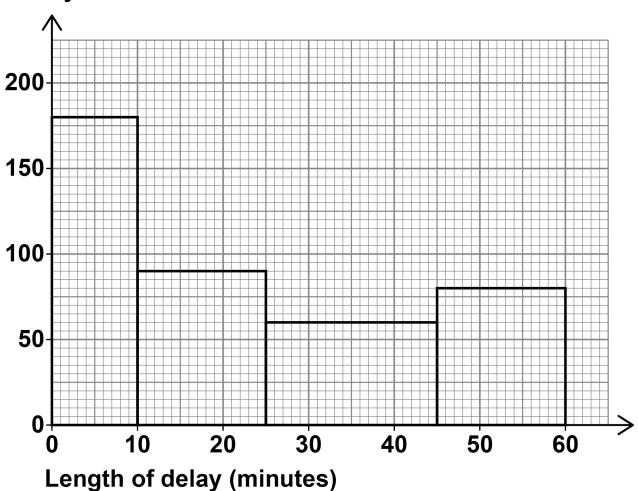


9 An airline records the length of delay, in minutes, whenever a flight is delayed.

The histogram represents this information for flights in MAY.

FLIGHTS IN MAY

Frequency density





Calculate an estimate for the number of flights in May that were delayed by MORE THAN 20 minutes. [3 marks]
Answer
Give a reason why it is NOT possible to calculate the exact value of the mean length of a delay from the histogram. [1 mark]

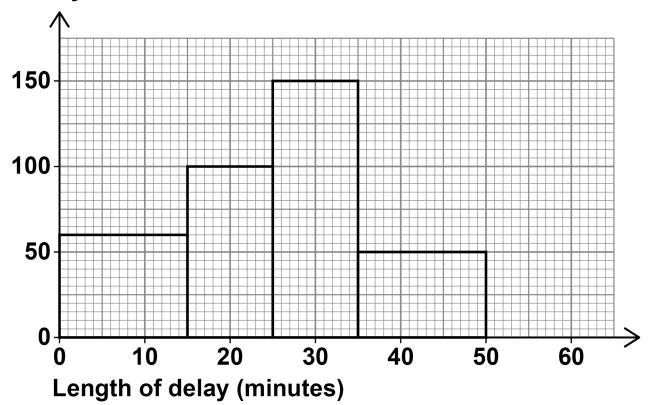


9 (b)(ii) Give a reason why the mean may NOT be representative for the length of a delay in May. [1 mark]

9 (c) The histogram represents the length of delay, in minutes, for flights in JUNE.

FLIGHTS IN JUNE

Frequency density





	The director of the airline says,	
	"The range for the length of a delay was SMALLER in June than in May."	
	Complete these sentences to comment on t statement. [2 marks]	his
	The director may be correct because	
	The discrete was a NOT be a server of be a server	
	The director may NOT be correct because	
[Turn c	over]	7



Jutta works in the finance department for a retailer.

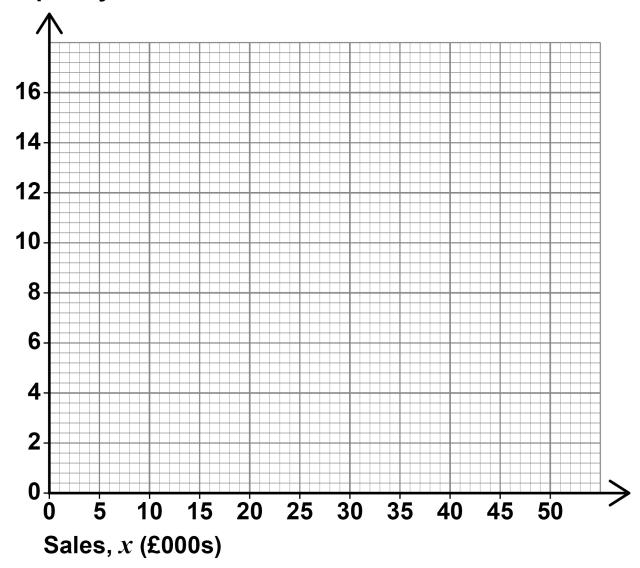
The table shows information about monthly sales figures over the past 40 months.

Sales, <i>x</i> (£000s)	Frequency
0 ≤ <i>x</i> < 10	2
10 ≤ <i>x</i> < 20	5
20 ≤ <i>x</i> < 30	11
30 ≤ <i>x</i> < 40	14
40 ≤ <i>x</i> < 50	8

10 (a) On the opposite page, draw a frequency polygon to represent Jutta's data. [3 marks]









10 (b)	Jutta chooses TWO of the months at random to examine their sales figures.
	Calculate the probability that the sales figure for BOTH months is at least £20 000
	You MUST show your working. [3 marks]
	Answar



10 (c)	Calculate an estimate of the median monthly sales.
	Give your answer to 3 significant figures. [3 marks]
	Answer £
	Allower 2
[Turn o	over]



7	A triathlon is an athletics event which has three sections,
	• a swim
	• a cycle
	• a run.
11 (a)	Owen wants to investigate whether there is a relationship between the times taken for the swim and cycle sections.
	Suggest a possible hypothesis for Owen's investigation. [1 mark]
5	Owen uses some of the results from the 2016 Olympic Games

Owen uses some or the results from the 2016 Olympic Games. (0) The table, on the opposite page, shows information for 8 different athletes.



ATHLETE	SWIM (MIN: SEC)	CYCLE (MIN:SEC)	RANK SWIM	RANK RANK SWIM CYCLE	DIFFERENCE	
Brownlee	17:24	55:04	1	3	-2	
Schoeman	17:25	55:01	2	1	1	
Murray	18:20	55:35	8	2	3	
Pereira	18:03	55:52	7	9	1	
Van Riel	17:27	55:03	4	2	2	
Mola	17:37	56:18	9	8	-2	
Royle	17:26	55:05	3	4	-1	
Bailie	17:31	56:11	5	7	-2	

Source: triathlon.org





Calculate the Spearman's rank correlation coefficient between the times taken to complete the swim and cycle sections. 11 (b) (i)

Use
$$r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)}$$

You may use the blank column in the table to help you. [3 marks]

[Turn over]

Answer





11 (b) (ii)	Interpret the value of the answer found in PART (b)(i) in context. [1 mark]
[Turn over]	



11 (c) The values of Spearman's rank correlation coefficient between other sections of the triathlon are shown in the table.

SECTIONS	SPEARMAN'S RANK CORRELATION COEFFICIENT
Swim and Run	-0.50
Cycle and Run	-0.26

Owen says,

"There is a STRONGER relationship between the swim and run sections than between the cycle and run sections."

Is Owen correct?

Tick (√) a box.

Yes

No

Give a reason for your answer. [1 mark]



					6
12	The weigh	nted mean o	of two numl	pers is cal	culated.
	One numl	oer has a va	alue of 16 a	nd a weigh	nting
	The other weighting	number ha of 3	s a value o	f 11 and a	
	Circle the numbers.	value of th [1 mark]	e weighted	mean of th	ne two
	12.5	13.5	14.5	19.7	
[Turn	over]				1



A soft drink is sold in cans which are filled by a machine.

Balasz takes a sample of cans every hour.

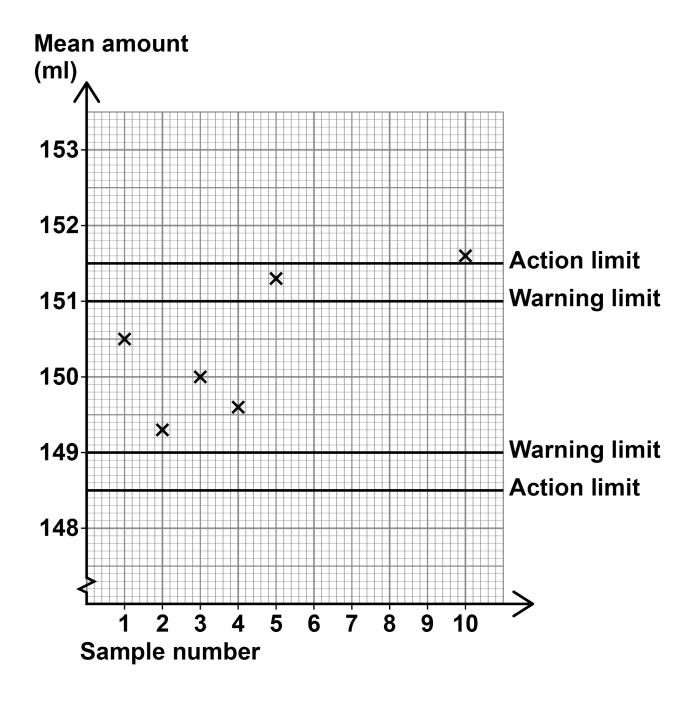
He finds the mean amount of drink in each sample.

The table shows the mean of each sample.

Sample number	Mean amount (ml)
1	150.5
2	149.3
3	150.0
4	149.6
5	151.3
6	150.8
7	149.8
8	151.2
9	149.3
10	151.6

The control chart, on the opposite page, shows some of the sample means and the warning and action limit lines.





13 (a) Complete the control chart. [2 marks]





13 ((h)	The	machine	ie	set so	that
10	(D)	1110	IIIaciiiic	13	301 30	, uiat,

- the mean amount of drink in a can is x ml
- ullet the standard deviation of the sample mean is y ml

The warning limit lines for the machine are drawn at x + 2y and x - 2y

Use the control chart, on page 51, to write down the value of x and work out the value of y [2 marks]

x =		
y =		



13 (c) (i)	Balasz actually took Sample 6 immediately after analysing Sample 5		
	Comment on whether this was appropriate.		
	Give a reason for your answer. [1 mark]		
13 (c) (ii)	Explain what action Balasz should take based on Sample 10 [1 mark]		
	$\left \frac{}{6} \right $		





In a talent show each contestant is given a mark by the judging panel.

The marks of ALL contestants can be modelled by a normal distribution with a mean of 60 and a standard deviation of 15

Daisy, Helen and Poppy each audition for the talent show.

Their standardised scores are shown in the table.

CONTESTANT	STANDARDISED SCORE
Daisy	-0.8
Helen	-2.2
Рорру	1.6

14 (a) To qualify for the next round in the competition a contestant needs a mark of 80 or more.

Show that Poppy qualifies for the next round.

Use

$$standardised score = \frac{value - mean}{standard deviation}$$

[2 marks]



14 (b)(i)	How does Daisy's mark compare with Helen's mark? [1 mark]



14 (b) (ii)	How does Daisy's mark compare with the marks of ALL contestants? [1 mark]		





15	Almaz wants to estimate the number of frogs in a lake.
	 She captures a sample of 380 frogs and tags them.
	She returns the frogs to the lake.
	 A week later she collects a second sample of 405 frogs.
	 In this second sample 3 of the frogs have tags.
15 (a)	Show that an ESTIMATE of the number of frogs in the lake is approximately 51 000 [2 marks]
15 (b)	Two years ago, Almaz estimated that there were 59 000 frogs in the lake.
	She concludes that the number of frogs in the lake has decreased by about 13%



Do you	u agree with Almaz?
Tick (v) a box.
	Yes
	No
Show	your working.
could	nould also refer to THREE factors that affect the accuracy of Almaz's estimate ing any assumptions made. [4 marks]
Factor	1



		Factor 2	
		Factor 3	
END	OF	QUESTIONS	6



Additional page, if required.		
Write the question numbers in the left-hand margin.		



Additional page, if required.		
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For Examiner's Use				
Question	Mark			
1				
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TOTAL				

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